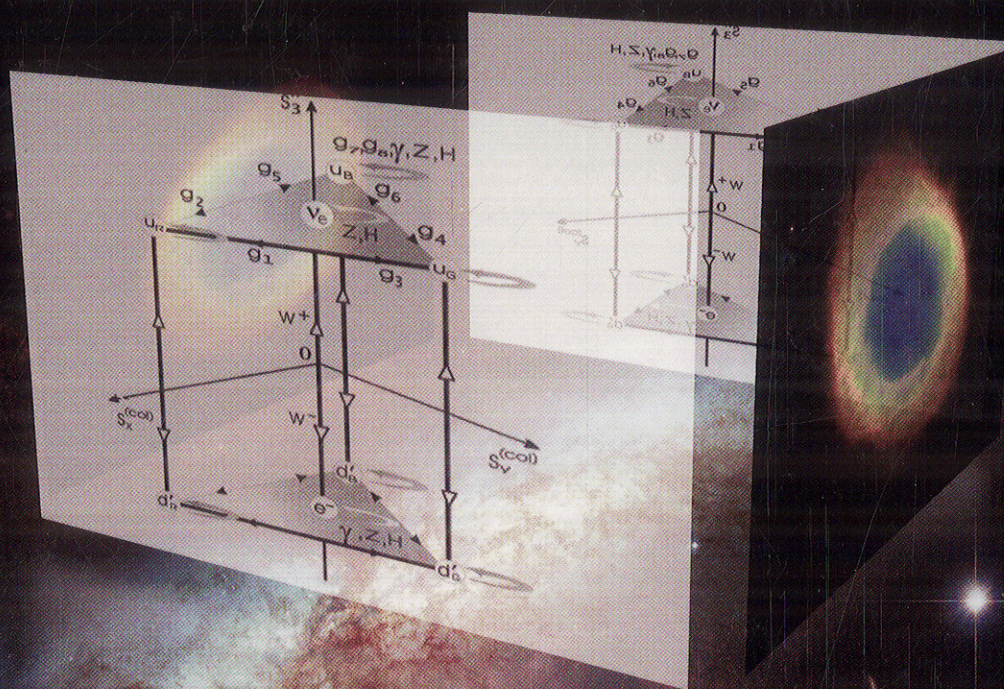


Advanced Particle Physics

Volume I

Particles, Fields, and
Quantum Electrodynamics



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Contents

Introduction	xi
Designations	xv
I Mathematical Prelude	1
1 Relativistic invariance	3
2 Three-dimensional world	9
2.1 Orthogonal transformation group $O(3)$	9
2.2 Tensor representations of the $SO(3)$ -group	14
3 The four-dimensional Minkowski space	21
3.1 The homogeneous Lorentz group	21
3.2 Classification of irreducible representations of the homogeneous Lorentz group	23
3.3 Tensor representations of the limited homogeneous Lorentz group	26
3.4 Spinor representations of the homogeneous Lorentz group	26
3.5 Poincare group and its representations	29
4 Lagrangian formulation of field theory	37
4.1 Principle of least action. Lagrange-Euler equations	37
4.2 Noether theorem and dynamic invariants	39
4.3 Energy-momentum tensor	42
4.4 Tensor of angular momentum	43
4.5 Electromagnetic current vector and electric charge	45
4.6 Isotopic spin	48
5 Discrete symmetry operations	53
5.1 Spatial inversion	53
5.2 Time inversion	56
5.3 Charge conjugation	59
5.4 G-parity	60
5.5 CPT theorem	61
Problems	65
References	69
II Birds's-Eye View on the Microworld	71
6 Fundamental interactions	73
6.1 Species of interactions	73
6.2 On the path to a unified field theory	87

7	Atoms–Nuclei–Nucleons	101
7.1	Atomism	101
7.2	Rutherford model of the atom	103
7.3	Structure of the atomic nucleus	111
8	From muon to gluon	113
9	Hadron families	125
9.1	Yukawa hypothesis	125
9.2	Isotopic multiplets	131
9.3	Unitary multiplets	140
10	Quark “atoms”	167
10.1	Hypothesis of fundamental triplets	167
10.2	X-ray photography of nucleons	173
10.3	Parton model	192
10.4	Quantum chromodynamics. The first acquaintance	197
10.5	Heavy quarks and flavor symmetries	207
11	Passing glance on the theory of electroweak interaction	219
11.1	Spontaneous symmetry breaking	219
11.2	Glashow–Weinberg–Salam theory	223
12	Fundamental particles of the Standard Model	237
13	Technical equipment of particle physics	245
13.1	Accelerators	245
13.2	Detectors	253
13.3	Neutrino Telescopes	259
	Problems	263
	References	269
III	Quantum Idyll—Free Fields	273
14	Scalar field	275
14.1	Klein-Gordon equation	275
14.2	Quantization	278
14.3	Production and destruction operators	280
14.4	Wave-corpuscle dualism	283
14.5	Commutation relations. Properties of commutator functions	287
14.6	Microcausality	290
14.7	Relativistically covariant scheme of the canonical quantization	291
14.8	Green function of the scalar field	293
14.9	Causal Green function	296
14.10	Chronological product. Convolution of operators	297
14.11	First-order equation for scalar particles	300

15 Particles with spin 1/2	309
15.1 Dirac equation	309
15.2 Calculating γ -matrix tracks	313
15.3 Relativistic covariance	314
15.4 Solutions of the free Dirac equation	321
15.5 Once more about particles spin	327
15.6 Polarization density matrix for Dirac particles	332
15.7 Dirac equation in the external electromagnetic field	335
15.8 Charge conjugation, spatial inversion, and time inversion for the Dirac field	339
15.9 Relativistic quantization scheme	342
15.10 Dirac field quantization (momentum space)	344
15.11 Dirac field quantization (configuration space)	348
15.12 Majorana equation	351
15.13 Quantization of Majorana field	355
15.14 Second quantized representation of discrete operations C , P , and T for particles with spin 1/2	358
15.15 Neutrino in the Dirac and Majorana theory	363
16 Massive vector field	371
16.1 Proca equation	371
16.2 Dynamic invariants of the vector field	374
16.3 Commutation relations in the Proca theory	379
16.4 Duffin-Kemmer equation for the vector field	380
17 Electromagnetic field	383
17.1 Maxwell equations	383
17.2 Dynamic invariants of the electromagnetic field	387
17.3 Electromagnetic field quantization	391
17.4 Quantization with use of an indefinite metric	394
17.5 Photon polarization	399
Problems	403
References	407
IV Quantum Electrodynamics	409
18 S-matrix	411
18.1 Equations and dynamic variables in the Heisenberg representation	411
18.2 Interaction representation	413
18.3 Scattering matrix	416
18.4 Representation of the S -matrix as the sum of normal products	423
18.5 Calculation of S -matrix elements	425
18.6 Feynman rules in coordinate space	430
18.7 Furry's theorem	436
18.8 Feynman rules in the momentum representation	438
18.9 Crossing symmetry	441
18.10 Cross section for unpolarized particles	447
18.11 Cross section for scattering by external fields	451
18.12 Decays of elementary particles	455
18.13 Cross section for polarized particles	458

18.14 Statistical hypothesis	462
19 Transmission of γ-radiation through matter	465
19.1 Photoeffect (nonrelativistic case)	465
19.2 Photoeffect (relativistic case)	470
19.3 Compton-effect (unpolarized case)	474
19.4 Compton-effect (polarized case)	482
19.5 Electron-positron pair production by the photon in the nucleus field . . .	487
19.6 Resume	495
20 Scattering of electrons and positrons	499
20.1 Bremsstrahlung	499
20.2 Radiation of long-wave photons. Infrared catastrophe	504
20.3 e^-e^+ -pair annihilation into two γ -quanta. e^-e^+ -pair production under annihilation of two γ -quanta	511
20.4 Positronium lifetime	518
20.5 Möller scattering $e^- + e^- \rightarrow e^- + e^-$	522
20.6 Processes $e^+ + e_{\nu}^- \rightarrow l + \bar{l}$ ($l = e^-, \mu^-, \tau^-$)	524
21 Radiative corrections	529
21.1 Calculations of integrals over virtual momenta	531
21.2 Regularization methods	536
21.3 Self-energy of the electron	543
21.4 Vacuum polarization	549
21.5 Vertex function of the third order	558
21.6 Radiative corrections to scattering of an electron by the Coulomb nucleus field	562
21.7 Anomalous magnetic moment of leptons	571
21.8 Lamb shift	580
22 Renormalization theory	587
22.1 Primitive divergent diagrams	588
22.2 Effective elements of Feynman diagrams	593
22.3 Ward identity	601
22.4 Extraction of divergences	604
22.5 QED renormalizability	609
22.6 Renormalization group	618
22.7 Consistency problems of the QED	620
Problems	623
References	627
Appendix: Natural system of units	631
Index	633