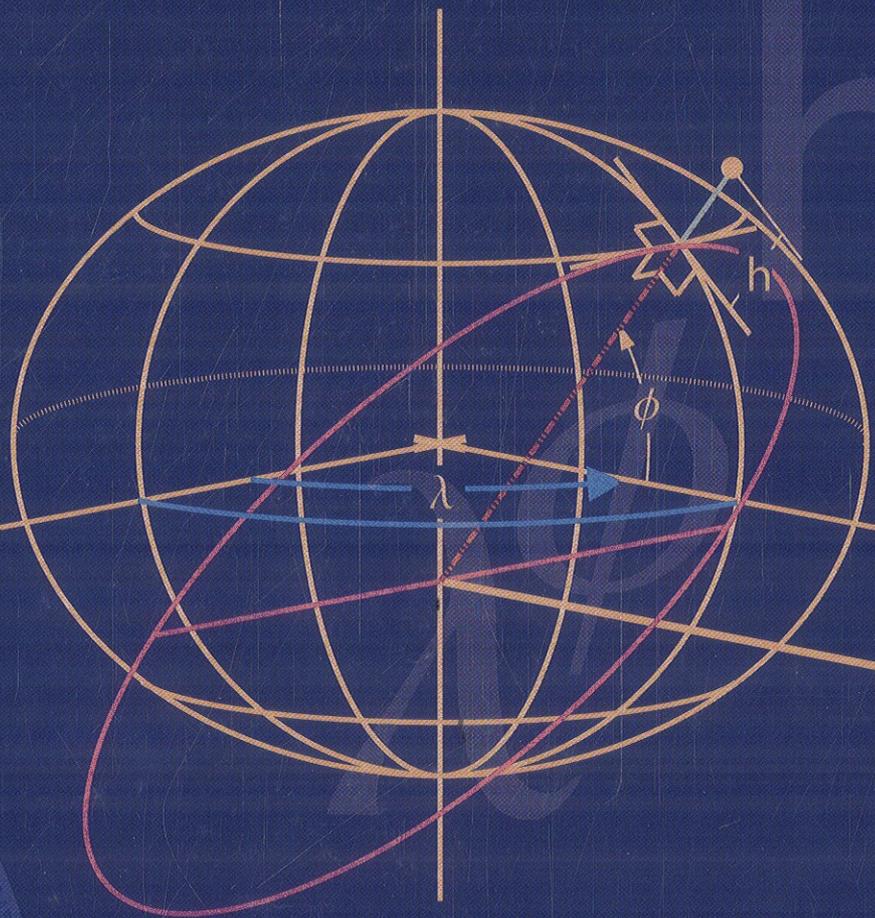


# Introduction to Geometrical and Physical Geodesy

## FOUNDATIONS OF GEOMATICS

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