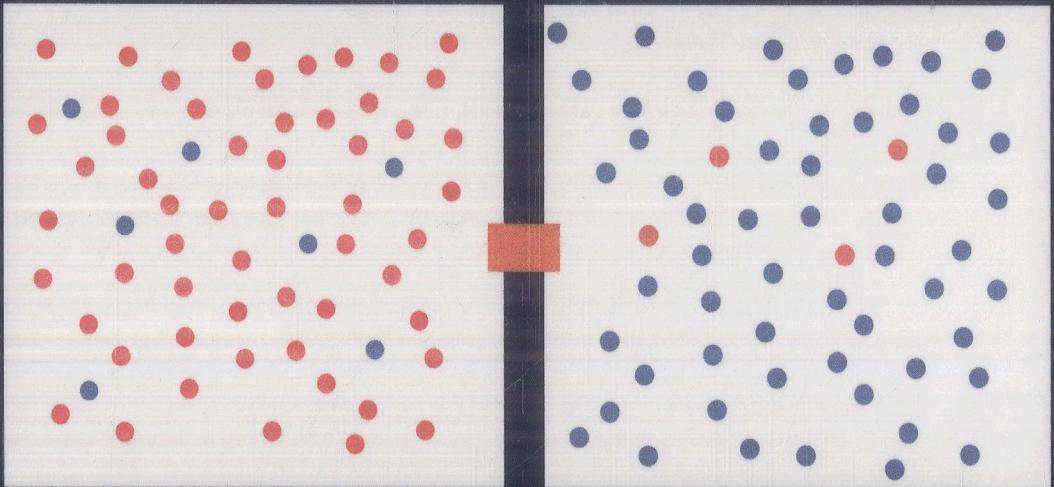


Michael E. Starzak

# Energy and Entropy

Equilibrium to Stationary States



Springer

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