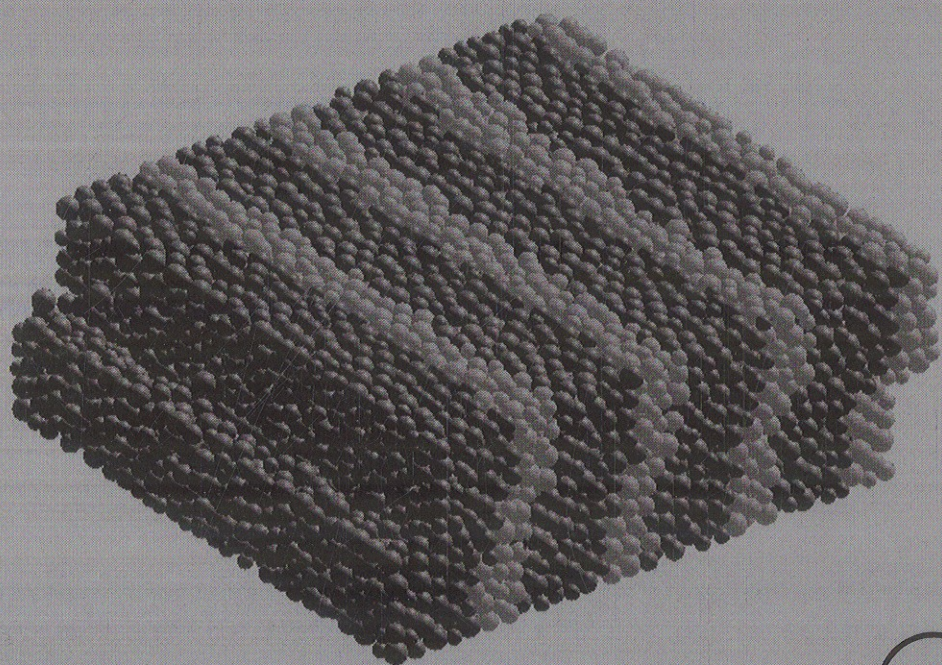


# PARTICULATE DISCRETE ELEMENT MODELLING

A Geomechanics Perspective

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APPLIED GEOTECHNICS VOLUME 4



Spon Press

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