

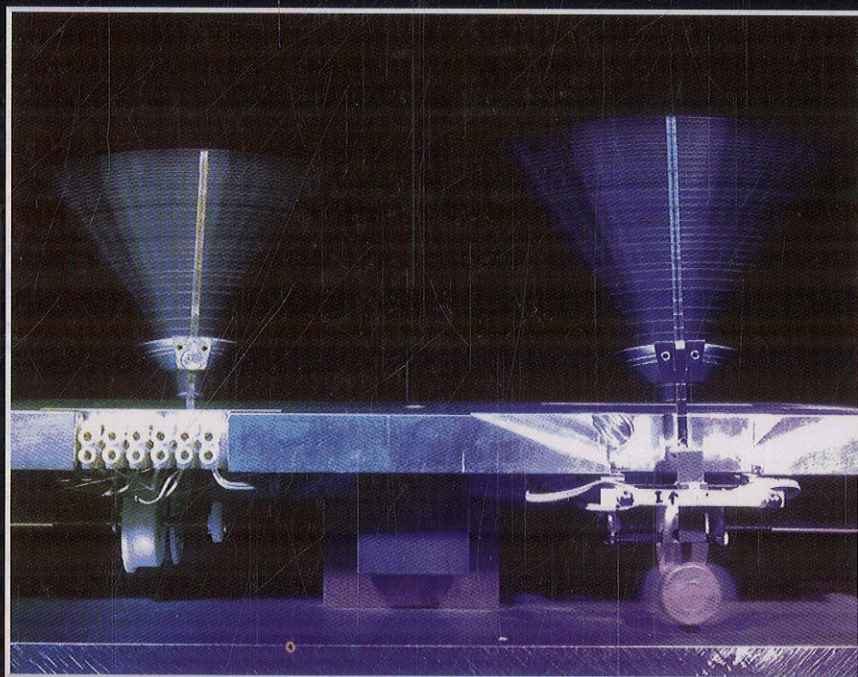
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DYNAMICS AND CONTROL OF HYBRID MECHANICAL SYSTEMS

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World Scientific

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