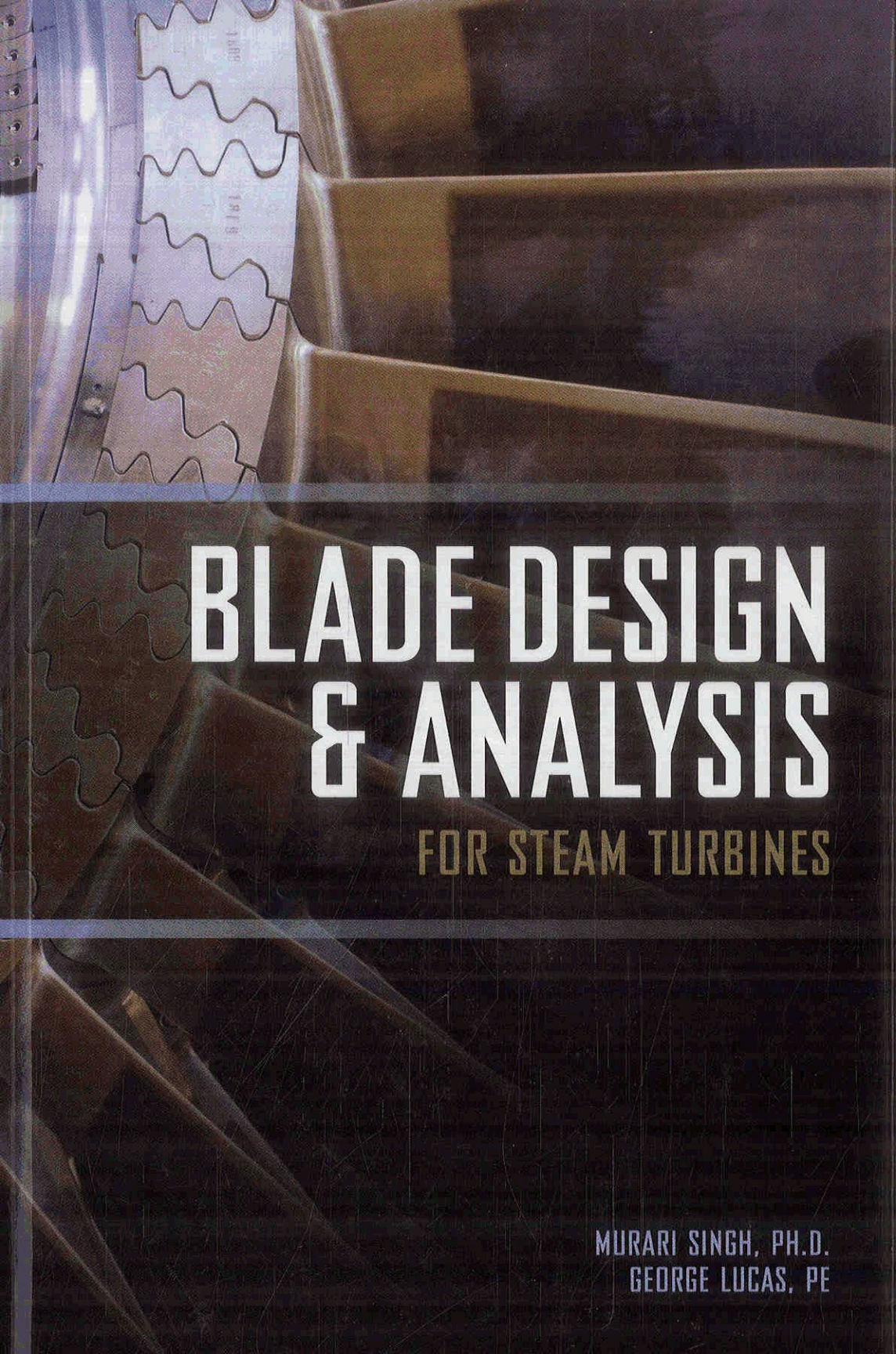


A close-up photograph of several steam turbine blades. The blades are arranged in a row, with their leading edges visible. The blades have a complex, curved shape with a wavy leading edge. The background is dark and out of focus, showing more blades and the internal structure of the turbine.

# BLADE DESIGN & ANALYSIS

FOR STEAM TURBINES

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