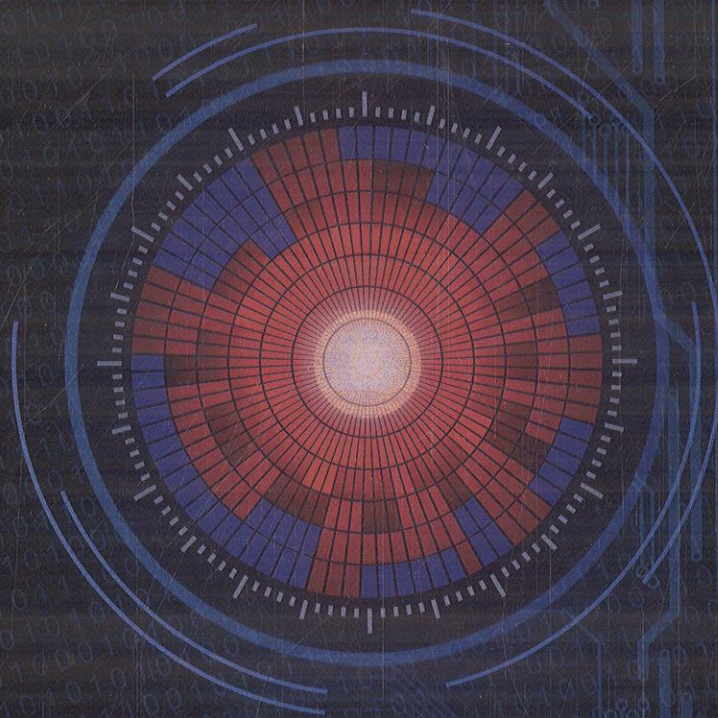


Computational and Physical Processes
in Mechanics and Thermal Sciences

COMPUTER METHODS FOR ENGINEERING WITH MATLAB® APPLICATIONS

SECOND EDITION

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CRC Press
Taylor & Francis Group

Contents

Preface to the Second Edition..... xiii

Preface to the First Edition xvii

Author xxi

Chapter 1 Introduction 1

 1.1 Introductory Remarks..... 1

 1.2 Numerical Solution..... 4

 1.3 Importance of Analytical Results..... 6

 1.4 Physical Considerations..... 9

 1.5 Application of Computer Methods to Engineering Problems 13

 1.6 Outline and Scope of the Book 15

 1.6.1 Basic Features 15

 1.6.2 Computer Programs 16

 1.6.3 Examples and Problems 16

 1.6.4 A Preview 17

Chapter 2 Basic Considerations in Computer Methods 21

 2.1 Introduction 21

 2.2 Computational Procedure..... 23

 2.2.1 Method Selection..... 23

 2.2.2 Programming Language..... 25

 2.2.3 Computer System 30

 2.2.4 Program Development..... 31

 2.2.4.1 Algorithm..... 31

 2.2.4.2 Available Programs..... 34

 2.2.4.3 Validation..... 35

 2.2.5 Serial versus Parallel Computing 35

 2.3 Numerical Errors and Accuracy..... 38

 2.3.1 Round-Off Error..... 40

 2.3.2 Truncation Error..... 42

 2.3.3 Accuracy of Numerical Results..... 45

 2.3.4 Numerical Stability 46

 2.4 Iterative Convergence 48

 2.4.1 Conditions for Convergence 49

 2.4.2 Rate of Convergence 50

 2.4.3 Termination of Iteration 50

2.5	Numerical Parameters	51
2.5.1	Step Size	52
2.5.2	Convergence Criterion.....	52
2.5.3	Other Arbitrarily Chosen Variables.....	53
2.6	Summary	54
	Problems.....	56
Chapter 3	A Review of MATLAB® Programming.....	59
3.1	Introduction	59
3.2	MATLAB® Environment	59
3.2.1	Basic Commands.....	59
3.2.2	Matrices.....	61
3.2.3	Arrays and Vectorization	62
3.2.4	Matrix Algebra.....	63
3.2.5	Polynomials.....	65
3.2.6	Root Solving.....	66
3.2.7	Linear Algebraic Equations	67
3.2.8	Curve Fitting	67
3.2.9	Flow Control.....	68
3.3	Ordinary Differential Equations	70
3.4	Input/Output	72
3.5	Script <i>m</i> -Files	76
3.6	Function <i>m</i> -Files.....	78
3.7	Plotting	81
3.8	Summary	82
	Problems.....	83
Chapter 4	Taylor Series and Numerical Differentiation	85
4.1	Introduction	85
4.2	Taylor Series	86
4.2.1	Basic Features	86
4.2.2	Finite Difference Calculus	87
4.3	Direct Approximation of Derivatives.....	95
4.4	Taylor-Series Approach and Accuracy	98
4.4.1	Finite Difference Approximation of the First Derivative	98
4.4.2	Second Derivative	99
4.4.3	Higher-Order Derivatives.....	101
4.4.4	Higher-Accuracy Approximations	103
4.5	Polynomial Representation.....	109
4.6	Partial Derivatives.....	112
4.7	Summary	117
	Problems.....	118

Chapter 5	Roots of Equations	121
5.1	Introduction	121
5.2	Search Method for Real Roots	123
5.3	Bisection Method.....	130
5.4	Regula Falsi and Secant Methods	133
5.4.1	Regula Falsi Method	133
5.4.2	Secant Method.....	134
5.5	Newton–Raphson Method and Modified Newton’s Method.....	138
5.5.1	Newton–Raphson Method.....	138
5.5.2	Modified Newton’s Method.....	141
5.5.3	Convergence	142
5.6	Successive Substitution Method	147
5.7	Other Methods.....	150
5.7.1	Müller’s Method	151
5.7.2	Iterative Factorization of Polynomials	153
5.7.3	Graeffe’s Method.....	158
5.7.4	Additional Methods.....	160
5.8	Summary	162
	Problems.....	162
 Chapter 6	 Numerical Solution of Simultaneous Algebraic Equations.....	 171
6.1	Introduction	171
6.2	Gaussian Elimination	174
6.2.1	Basic Approach	174
6.2.2	Computational Procedure.....	175
6.2.3	Solution Accuracy	178
6.2.3.1	Ill-Conditioned Set	179
6.2.3.2	Error Correction	179
6.2.3.3	Pivoting.....	180
6.2.4	Matrix Inversion and Determinant Evaluation.....	180
6.2.5	Tridiagonal Systems	181
6.3	Gauss–Jordan Elimination	189
6.3.1	Mathematical Procedure	189
6.3.2	Computational Scheme.....	190
6.4	Compact Methods.....	194
6.4.1	Matrix Decomposition	194
6.4.2	Matrix Decomposition in MATLAB®	196
6.4.3	Crout’s Method.....	197
6.5	Numerical Solution of Linear Systems by Matrix Inversion	201
6.5.1	Computational Procedure.....	202
6.5.2	Additional Considerations	204

6.6	Iterative Methods.....	206
6.6.1	Basic Approach	206
6.6.2	Jacobi and Gauss–Seidel Methods	207
6.6.3	Convergence	208
6.6.4	An Example.....	209
6.6.5	Relaxation Methods.....	210
6.7	Homogeneous Linear Equations	214
6.7.1	The Eigenvalue Problem	215
6.7.2	The Power Method	220
6.7.2.1	Largest Eigenvalue.....	220
6.7.2.2	Smallest Eigenvalue.....	221
6.7.2.3	Intermediate Eigenvalues.....	222
6.7.3	Other Methods.....	224
6.8	Solution of Simultaneous Nonlinear Equations	225
6.8.1	Newton–Raphson Method.....	226
6.8.2	Modified Jacobi and Gauss–Seidel Methods	227
6.8.3	Convergence	228
6.9	Summary	234
	Problems.....	235

Chapter 7	Numerical Curve Fitting and Interpolation.....	247
7.1	Introduction	247
7.1.1	Exact and Best Fit.....	247
7.1.2	Interpolation and Extrapolation	249
7.1.3	Basic Approach	249
7.1.4	Use of MATLAB® Commands	251
7.2	Exact Fit and Interpolation	251
7.2.1	Exact Fit with an n th-Order Polynomial	252
7.2.2	Uniformly Spaced Independent Variable	255
7.3	Lagrange Interpolation	258
7.4	Newton’s Divided-Difference Interpolating Polynomial.....	262
7.4.1	General Formulas.....	263
7.4.2	Uniformly Spaced Data.....	266
7.4.3	Extrapolation	268
7.5	Numerical Interpolation with Splines	272
7.6	Method of Least Squares for a Best Fit	278
7.6.1	Basic Considerations	278
7.6.2	Linear Regression.....	281
7.6.3	Best Fit with a Polynomial	283
7.6.4	Nonpolynomial Forms.....	285
7.6.4.1	Linearization.....	286
7.7	Function of Two or More Independent Variables	293
7.7.1	Exact Fit	294
7.7.2	Best Fit.....	296

7.8	Summary	299
	Problems	300
Chapter 8	Numerical Integration	307
8.1	Introduction	307
8.1.1	Engineering Examples	309
8.2	Rectangular and Trapezoidal Rules for Integration	310
8.2.1	The Rectangular Rule	311
8.2.2	The Trapezoidal Rule	312
8.2.3	Truncation Error	313
8.2.3.1	Rectangular Rule	315
8.2.3.2	Trapezoidal Rule	315
8.2.3.3	Total Error	316
8.2.3.4	Accuracy	318
8.3	Simpson's Rules for Numerical Integration	322
8.3.1	Simpson's One-Third Rule	322
8.3.2	Simpson's Three-Eighths Rule	324
8.3.3	Truncation Errors	326
8.3.4	Use of MATLAB® Integration Commands	330
8.4	Higher-Accuracy Methods	332
8.4.1	Richardson Extrapolation	332
8.4.2	Romberg Integration	334
8.4.3	Higher-Order Newton–Cotes Formulas	336
8.5	Integration with Segments of Unequal Width	340
8.5.1	Unequally Spaced Data	340
8.5.2	Adaptive Quadrature	341
8.5.3	Gauss Quadrature	343
8.6	Numerical Integration of Improper Integrals	349
8.6.1	Integrals with Infinite Limits	350
8.6.2	Singular Integrand	351
8.6.3	Multiple Integrals	356
8.7	Summary	356
	Problems	357
Chapter 9	Numerical Solution of Ordinary Differential Equations	365
9.1	Introduction	365
9.1.1	Initial and Boundary Value Problems	366
9.1.2	Reduction of Higher-Order Equations to First-Order Equations	366
9.1.3	Solution Methods	369
9.2	Euler's Method	370
9.2.1	Computational Formula and Physical Interpretation of the Method	370

9.2.2	Solution of a System of Equations.....	372
9.2.3	Errors, Convergence, and Stability	374
9.3	Improvements in Euler's Method	380
9.3.1	Heun's Method	380
9.3.2	Modified Euler's Method.....	383
9.4	Runge–Kutta Methods.....	384
9.4.1	Computational Formulas	386
9.4.2	Truncation Error and Accuracy	389
9.4.3	System of Equations	391
9.5	Multistep Methods	397
9.5.1	Adams Multistep Methods	397
9.5.2	Additional Considerations	401
9.6	Predictor–Corrector Methods.....	401
9.6.1	Basic Features	402
9.6.2	Adams Method	403
9.6.3	Milne's Method	404
9.6.4	Hamming's Method.....	405
9.6.5	Accuracy and Stability of Predictor–Corrector Methods.....	406
9.6.5.1	Truncation Errors.....	406
9.6.5.2	Step Size	408
9.6.5.3	Stability.....	409
9.6.6	Simultaneous Equations	410
9.6.7	Concluding Remarks on Predictor–Corrector Methods.....	410
9.7	Boundary-Value Problems.....	416
9.7.1	Shooting Methods	417
9.7.1.1	Linear Equations.....	419
9.7.2	Finite Difference Methods	420
9.7.3	Eigenvalue Problems	423
9.8	Summary	430
	Problems.....	432

Chapter 10 Numerical Solution of Partial Differential Equations.....445

10.1	Introduction	445
10.1.1	Classification	445
10.1.2	Examples	446
10.1.3	Basic Considerations	448
10.2	Parabolic PDEs.....	449
10.2.1	Numerical Solution with an Explicit Scheme	450
10.2.2	Stability of Euler's (FTCS) Method	453
10.2.3	Implicit Methods	454
10.2.4	Other Methods and Considerations.....	456
10.2.5	Multidimensional Problems	458

10.3	Elliptic PDEs	467
10.3.1	Finite Difference Approach.....	467
10.3.2	Numerical Solution by Iterative and Direct Methods.....	472
10.3.2.1	Point Relaxation.....	474
10.3.2.2	Direct Methods	476
10.3.3	Other Methods.....	476
10.3.4	Other Geometries and Boundary Conditions.....	477
10.3.5	Finite Element and Other Solution Methods.....	480
10.4	Hyperbolic PDEs	489
10.4.1	Basic Aspects	489
10.4.2	Method of Characteristics	489
10.4.3	Finite Difference Methods	490
10.5	Summary	500
	Problems.....	502
Appendix A: Some Common Commands in MATLAB®		509
Appendix B: Computer Programs in MATLAB®		513
Appendix C: Computer Programs in FORTRAN		553
References		591
Index.....		595