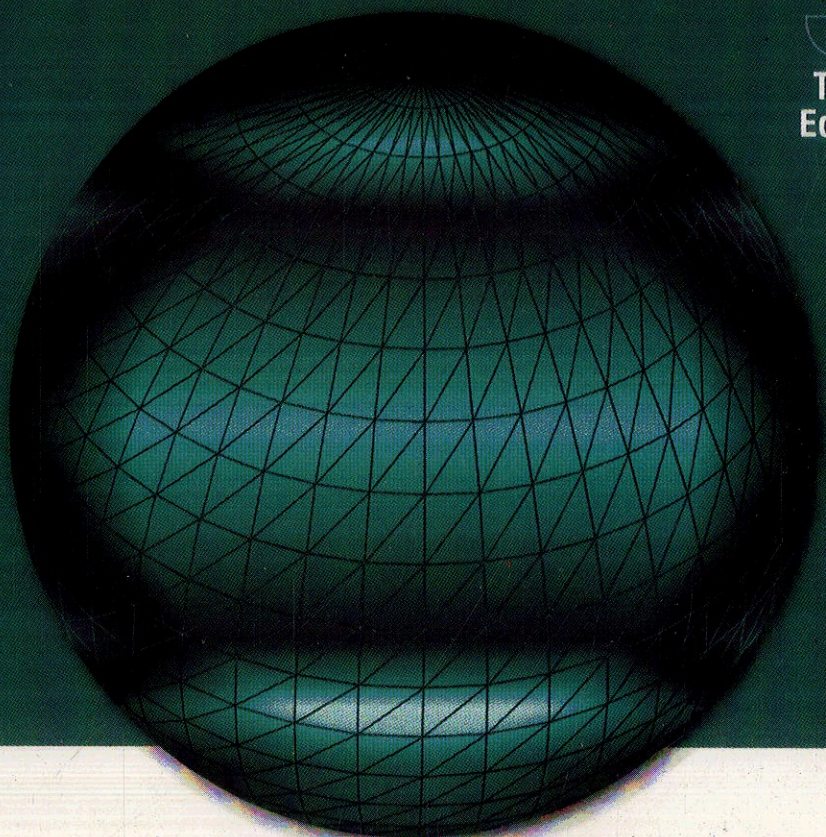


The **McGraw-Hill** Companies

3
Third
Edition



Advanced Mechanics of **SOLIDS**

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