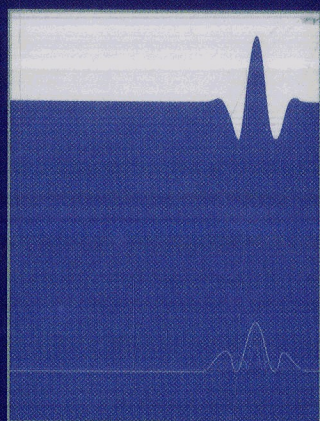


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Sparse Image and Signal Processing



**Wavelets, Curvelets,
Morphological
Diversity**

CAMBRIDGE

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