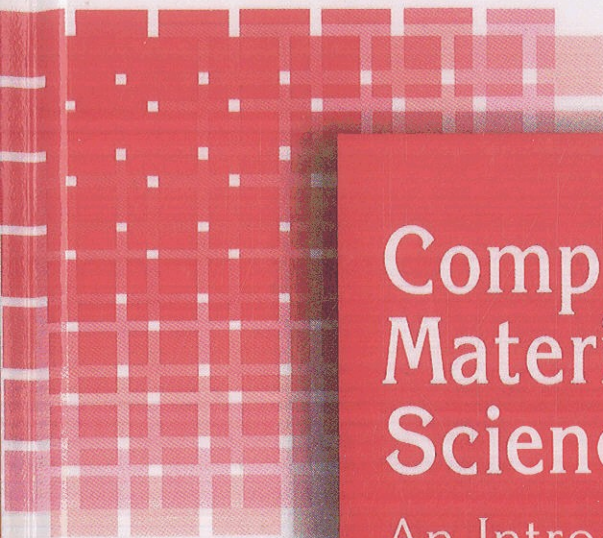
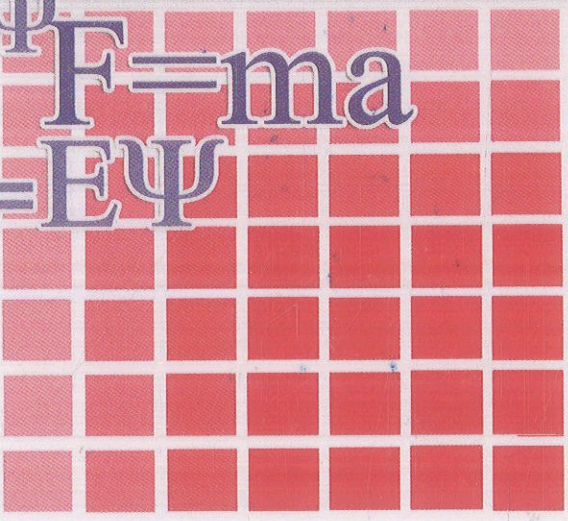




Computational Materials Science

An Introduction

June Gunn Lee


$$\begin{array}{l} H\Psi = E\Psi \\ F = ma \\ H\Psi = E\Psi \end{array}$$



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