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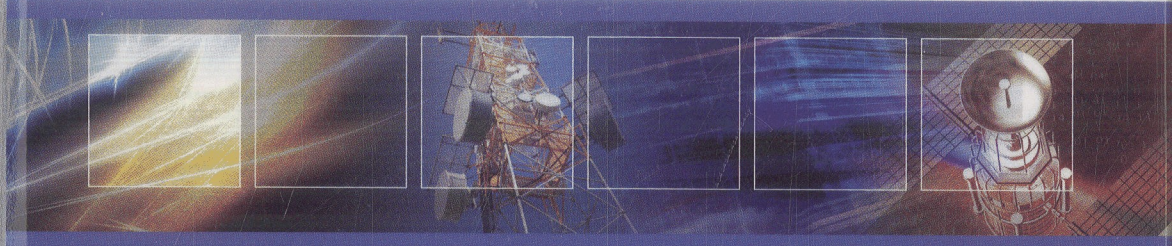
Wireless Multi-Antenna Channels

Modeling and Simulation



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