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# INDUCING ROBUST CHAOS IN ELECTRONIC CIRCUITS

A low-power and reversible technique to jam electronic circuits using chaos theory and the concept of resonance



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