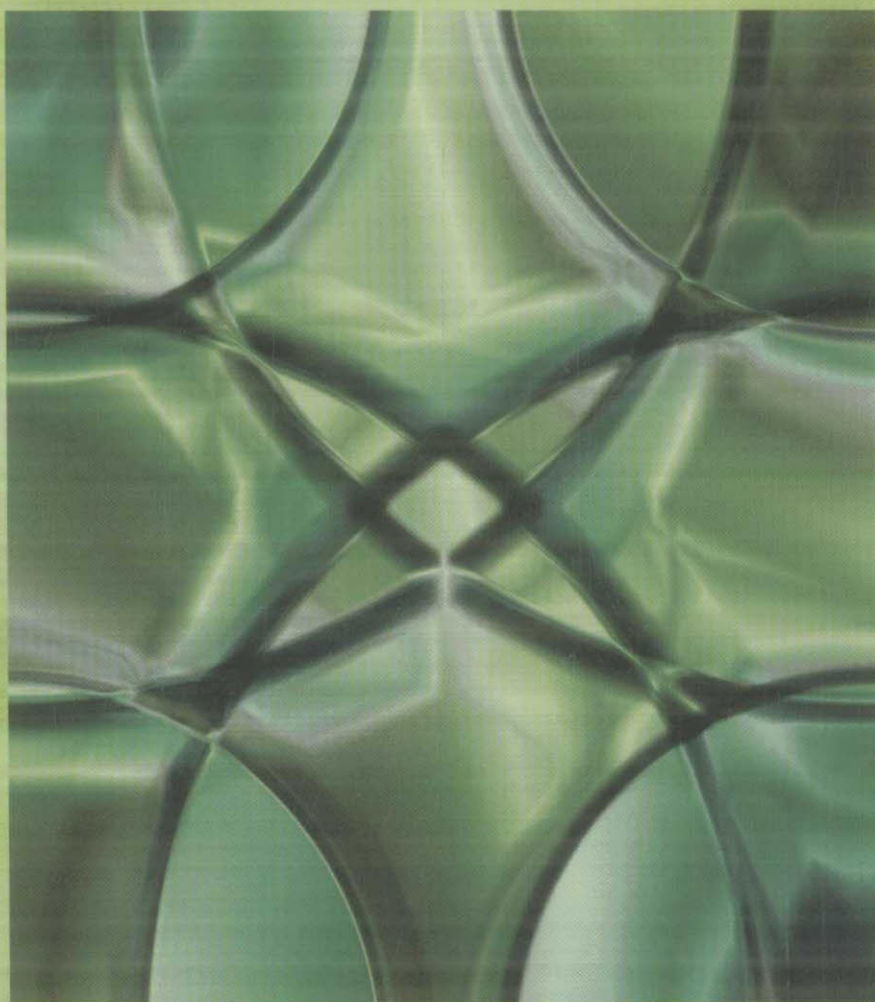


Fundamentals of
CONDENSED MATTER
AND CRYSTALLINE
PHYSICS



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