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The companion website www.guilford.com/grimm-materials provides datasets and syntax for the book's examples, along with additional code in SAS/R for linear mixed-effects modeling.