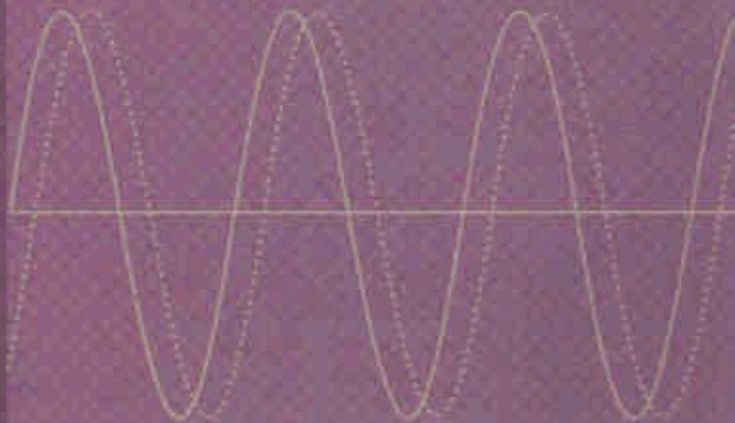




S. GRAHAM KELLY

FUNDAMENTALS OF MECHANICAL VIBRATIONS

SECOND EDITION



McGRAW-HILL INTERNATIONAL EDITIONS
Mechanical Engineering Series

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