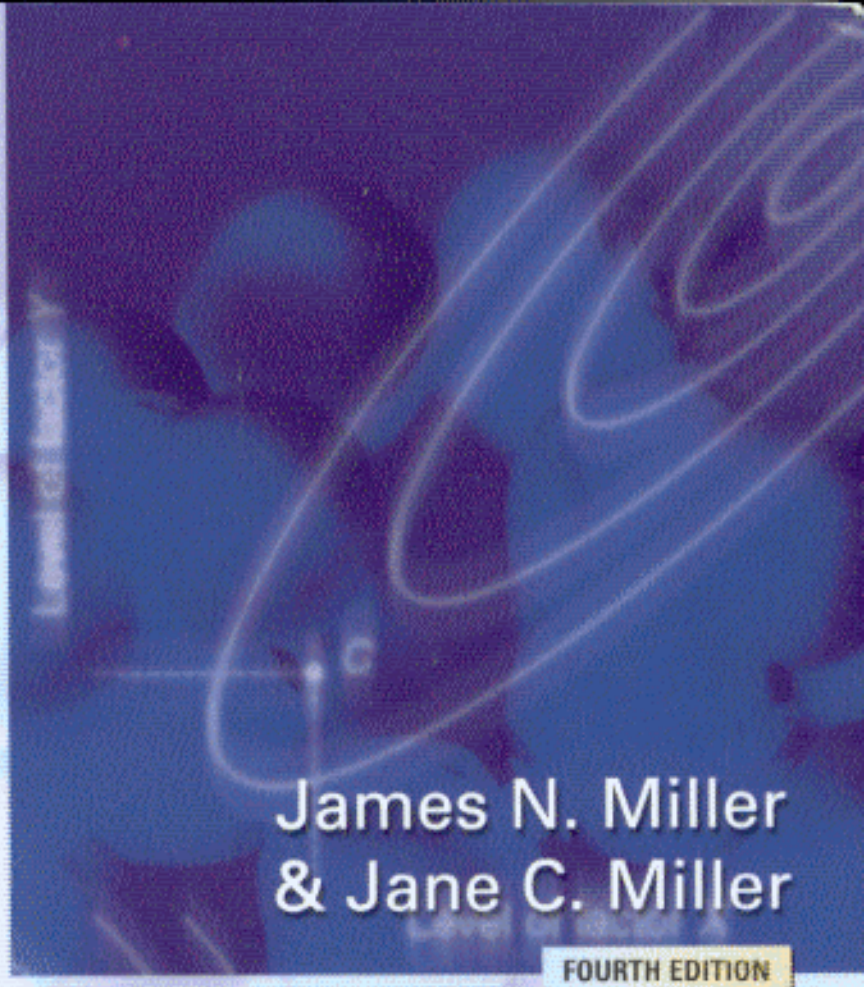

James N. Miller
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FOURTH EDITION

Statistics and Chemometrics for Analytical Chemistry

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