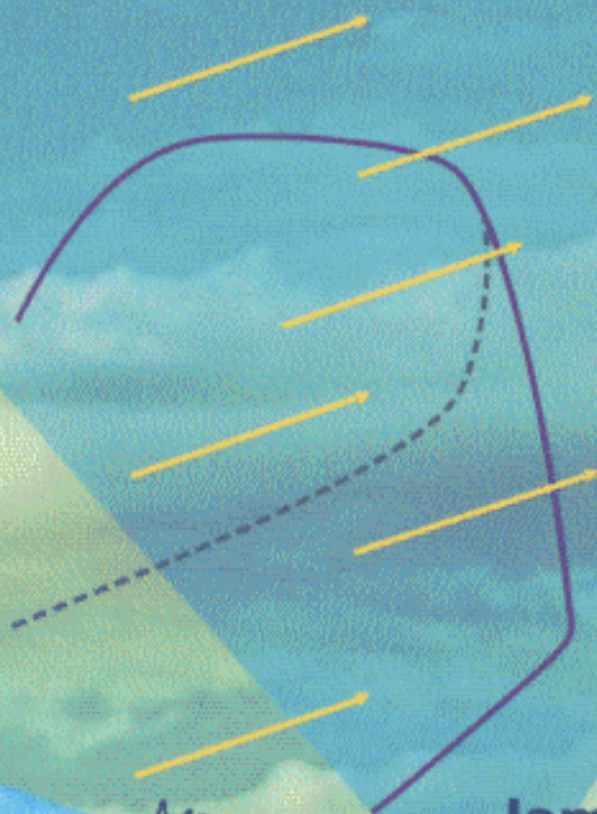


A MATHEMATICAL VIEW OF INTERIOR-POINT METHODS IN CONVEX OPTIMIZATION



James Renegar

MPS-SIAM Series on Optimization

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