

# HANDBOOK OF SHOCK WAVES

## EDITORS

Gabi Ben-Dor  
Ozer Igra  
Tov Elperin

## VOLUME **1**

Theoretical, Experimental, and  
Numerical Techniques



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