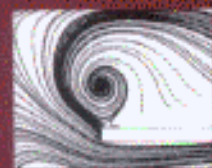
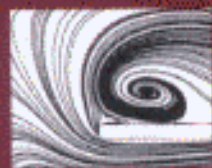


COMPUTATION OF UNSTEADY INTERNAL FLOWS

Fundamental Methods with Case Studies

Paul G. Tucker



KLUWER ACADEMIC PUBLISHERS

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