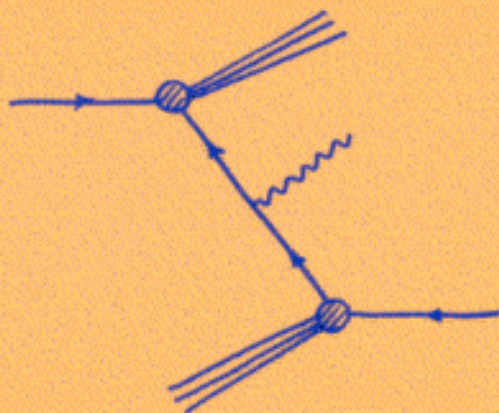


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# Unification and Supersymmetry

## The Frontiers of Quark-Lepton Physics

Third Edition



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