## Automatic Control Systems





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CD-ROM

Frequency-Domain Plots CD-ROM

➤ APPENDIX H General Nyquist Criterion CD-ROM

➤ APPENDIX G

► APPENDIX I Discrete-Data Control Systems CD-ROM

APPENDIX J z-Transform Table CD-ROM

APPENDIX K

ACSYS 2002: Description of the Software CD-ROM

ANSWERS TO SELECTED PROBLEMS