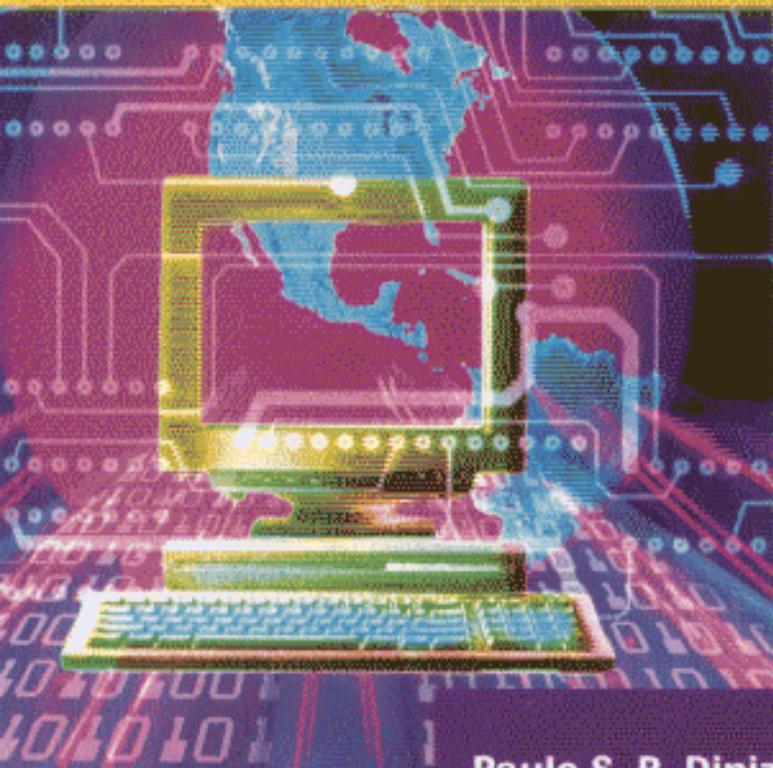


Digital Signal Processing

System Analysis and Design



**Paulo S. R. Diniz, Eduardo A. B. da Silva,
and Sergio L. Netto**

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