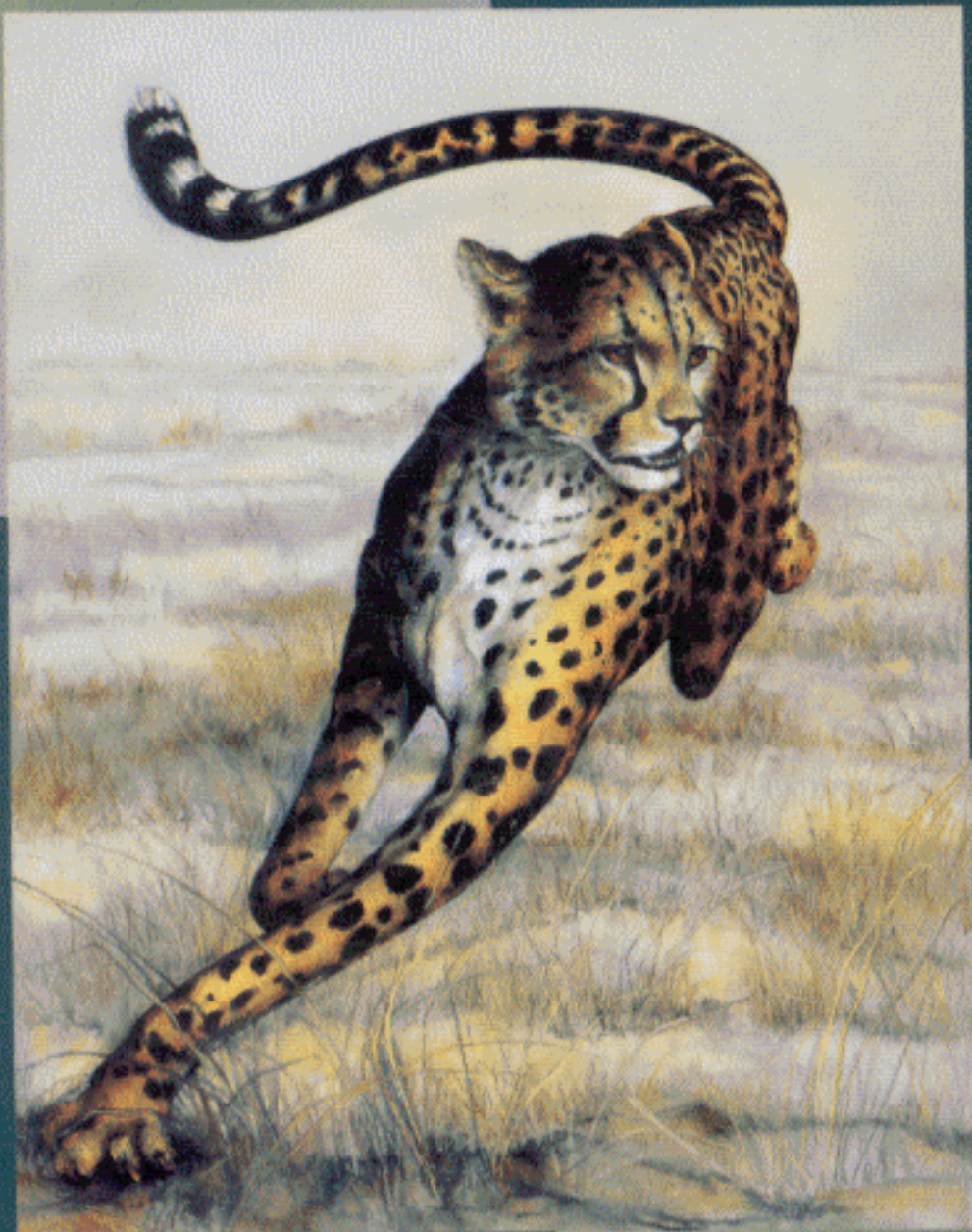


INTERNATIONAL EDITION

Continuous and Discrete Control Systems

Modeling, Identification,



Design, and Implementation

John Dorsey

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