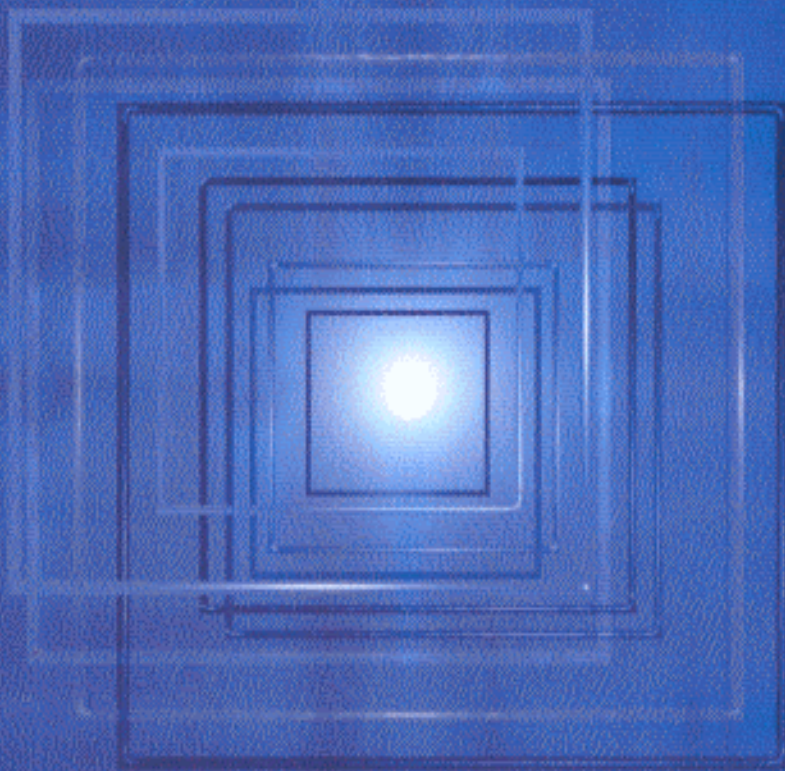

Applied Bayesian Modelling



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Contents

Preface	xi
Chapter 1 The Basis for, and Advantages of, Bayesian Model Estimation via Repeated Sampling	1
1.1 Introduction	1
1.2 Gibbs sampling	5
1.3 Simulating random variables from standard densities	12
1.4 Monitoring MCMC chains and assessing convergence	18
1.5 Model assessment and sensitivity	20
1.6 Review	27
References	28
Chapter 2 Hierarchical Mixture Models	31
2.1 Introduction: Smoothing to the Population	31
2.2 General issues of model assessment: marginal likelihood and other approaches	32
2.2.1 Bayes model selection using marginal likelihoods	33
2.2.2 Obtaining marginal likelihoods in practice	35
2.2.3 Approximating the posterior	37
2.2.4 Predictive criteria for model checking and selection	39
2.2.5 Replicate sampling	40
2.3 Ensemble estimates: pooling over similar units	41
2.3.1 Mixtures for Poisson and binomial data	43
2.3.2 Smoothing methods for continuous data	51
2.4 Discrete mixtures and Dirichlet processes	58
2.4.1 Discrete parametric mixtures	58
2.4.2 DPP priors	60
2.5 General additive and histogram smoothing priors	67
2.5.1 Smoothness priors	68
2.5.2 Histogram smoothing	69
2.6 Review	74
References	75
Exercises	78

Chapter 3	Regression Models	79
3.1	Introduction: Bayesian regression	79
3.1.1	Specifying priors: constraints on parameters	80
3.1.2	Prior specification: adopting robust or informative priors	81
3.1.3	Regression models for overdispersed discrete outcomes	82
3.2	Choice between regression models and sets of predictors in regression	84
3.2.1	Predictor selection	85
3.2.2	Cross-validation regression model assessment	86
3.3	Polytomous and ordinal regression	98
3.3.1	Multinomial logistic choice models	99
3.3.2	Nested logit specification	100
3.3.3	Ordinal outcomes	101
3.3.4	Link functions	102
3.4	Regressions with latent mixtures	110
3.5	General additive models for nonlinear regression effects	115
3.6	Robust Regression Methods	118
3.6.1	Binary selection models for robustness	119
3.6.2	Diagnostics for discordant observations	120
3.7	Review	126
	References	129
	Exercises	132
Chapter 4	Analysis of Multi-Level Data	135
4.1	Introduction	135
4.2	Multi-level models: univariate continuous and discrete outcomes	137
4.2.1	Discrete outcomes	139
4.3	Modelling heteroscedasticity	145
4.4	Robustness in multi-level modelling	151
4.5	Multi-level data on multivariate indices	156
4.6	Small domain estimation	163
4.7	Review	167
	References	168
	Exercises	169
Chapter 5	Models for Time Series	171
5.1	Introduction	171
5.2	Autoregressive and moving average models under stationarity and non-stationarity	172
5.2.1	Specifying priors	174
5.2.2	Further types of time dependence	179
5.2.3	Formal tests of stationarity in the AR(1) model	180
5.2.4	Model assessment	182
5.3	Discrete Outcomes	191
5.3.1	Auto regression on transformed outcome	193

5.3.2	INAR models for counts	193
5.3.3	Continuity parameter models	195
5.3.4	Multiple discrete outcomes	195
5.4	Error correction models	200
5.5	Dynamic linear models and time varying coefficients	203
5.5.1	State space smoothing	205
5.6	Stochastic variances and stochastic volatility	210
5.6.1	ARCH and GARCH models	210
5.6.2	Stochastic volatility models	211
5.7	Modelling structural shifts	215
5.7.1	Binary indicators for mean and variance shifts	215
5.7.2	Markov mixtures	216
5.7.3	Switching regressions	216
5.8	Review	221
	References	222
	Exercises	225
Chapter 6	Analysis of Panel Data	227
6.1	Introduction	227
6.1.1	Two stage models	228
6.1.2	Fixed vs. random effects	230
6.1.3	Time dependent effects	231
6.2	Normal linear panel models and growth curves for metric outcomes	231
6.2.1	Growth Curve Variability	232
6.2.2	The linear mixed model	234
6.2.3	Variable autoregressive parameters	235
6.3	Longitudinal discrete data: binary, ordinal and multinomial and Poisson panel data	243
6.3.1	Beta-binomial mixture for panel data	244
6.4	Panels for forecasting	257
6.4.1	Demographic data by age and time period	261
6.5	Missing data in longitudinal studies	264
6.6	Review	268
	References	269
	Exercises	271
Chapter 7	Models for Spatial Outcomes and Geographical Association	273
7.1	Introduction	273
7.2	Spatial regressions for continuous data with fixed interaction schemes	275
7.2.1	Joint vs. conditional priors	276
7.3	Spatial effects for discrete outcomes: ecological analysis involving count data	278
7.3.1	Alternative spatial priors in disease models	279
7.3.2	Models recognising discontinuities	281
7.3.3	Binary Outcomes	282

7.4	Direct modelling of spatial covariation in regression and interpolation applications	289
7.4.1	Covariance modelling in regression	290
7.4.2	Spatial interpolation	291
7.4.3	Variogram methods	292
7.4.4	Conditional specification of spatial error	293
7.5	Spatial heterogeneity: spatial expansion, geographically weighted regression, and multivariate errors	298
7.5.1	Spatial expansion model	298
7.5.2	Geographically weighted regression	299
7.5.3	Varying regressions effects via multivariate priors	300
7.6	Clustering in relation to known centres	303
7.6.1	Areas vs. case events as data	306
7.6.2	Multiple sources	306
7.7	Spatio-temporal models	310
7.7.1	Space-time interaction effects	312
7.7.2	Area Level Trends	312
7.7.3	Predictor effects in spatio-temporal models	313
7.7.4	Diffusion processes	314
7.8	Review	316
	References	317
	Exercises	320
Chapter 8	Structural Equation and Latent Variable Models	323
8.1	Introduction	323
8.1.1	Extensions to other applications	325
8.1.2	Benefits of Bayesian approach	326
8.2	Confirmatory factor analysis with a single group	327
8.3	Latent trait and latent class analysis for discrete outcomes	334
8.3.1	Latent class models	335
8.4	Latent variables in panel and clustered data analysis	340
8.4.1	Latent trait models for continuous data	341
8.4.2	Latent class models through time	341
8.4.3	Latent trait models for time varying discrete outcomes	343
8.4.4	Latent trait models for clustered metric data	343
8.4.5	Latent trait models for mixed outcomes	344
8.5	Latent structure analysis for missing data	352
8.6	Review	357
	References	358
	Exercises	360
Chapter 9	Survival and Event History Models	361
9.1	Introduction	361
9.2	Continuous time functions for survival	363
9.3	Accelerated hazards	370
9.4	Discrete time approximations	372
9.4.1	Discrete time hazards regression	375

9.4.2	Gamma process priors	381
9.5	Accounting for frailty in event history and survival models	384
9.6	Counting process models	388
9.7	Review	393
	References	394
	Exercises	396
Chapter 10	Modelling and Establishing Causal Relations: Epidemiological Methods and Models	397
10.1	Causal processes and establishing causality	397
10.1.1	Specific methodological issues	398
10.2	Confounding between disease risk factors	399
10.2.1	Stratification vs. multivariate methods	400
10.3	Dose-response relations	413
10.3.1	Clustering effects and other methodological issues	416
10.3.2	Background mortality	427
10.4	Meta-analysis: establishing consistent associations	429
10.4.1	Priors for study variability	430
10.4.2	Heterogeneity in patient risk	436
10.4.3	Multiple treatments	439
10.4.4	Publication bias	441
10.5	Review	443
	References	444
	Exercises	447
Index		449