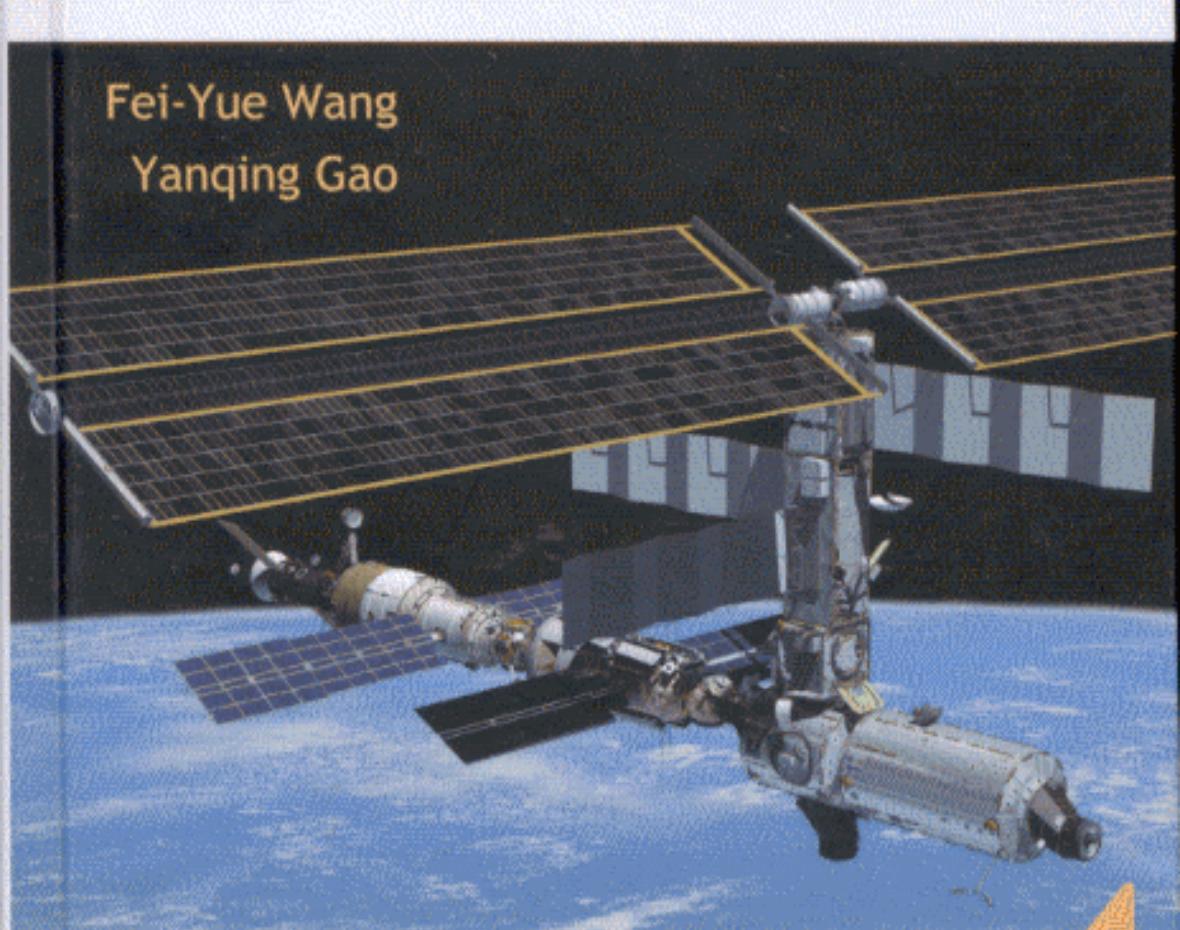


# Advanced Studies of Flexible Robotic Manipulators

*Modeling, Design, Control and Applications*

Fei-Yue Wang  
Yanqing Gao



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