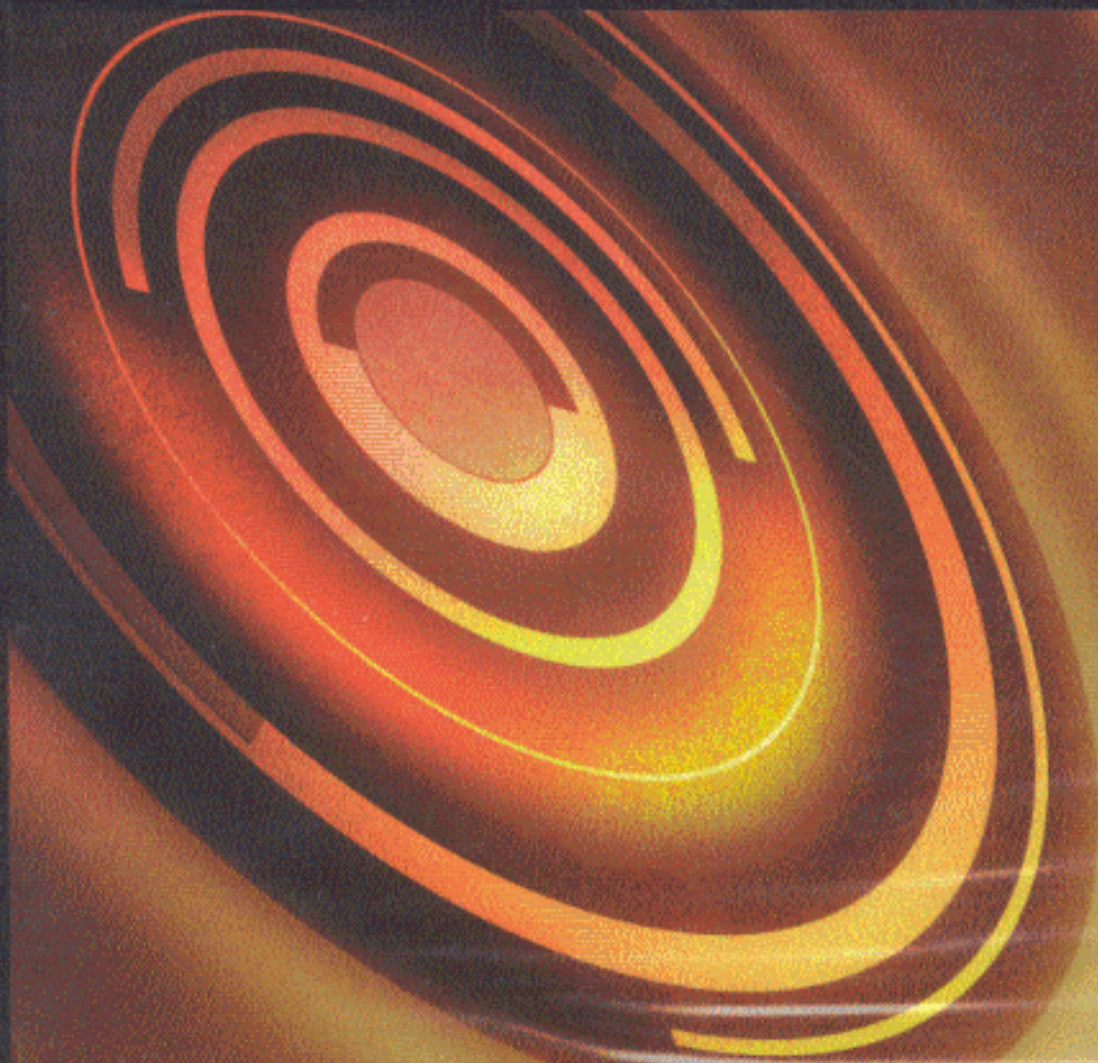


INTERNATIONAL EDITION

SIGNALS, SYSTEMS, AND TRANSFORMS

THIRD EDITION



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