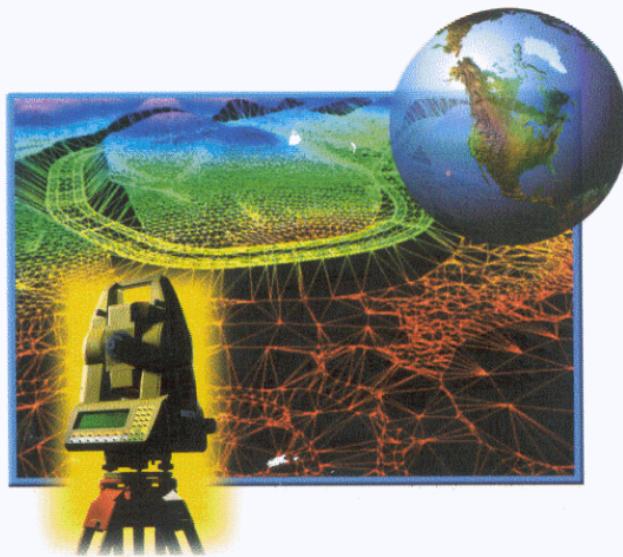


INTERNATIONAL EDITION

TENTH EDITION

Elementary Surveying

An Introduction to Geomatics



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