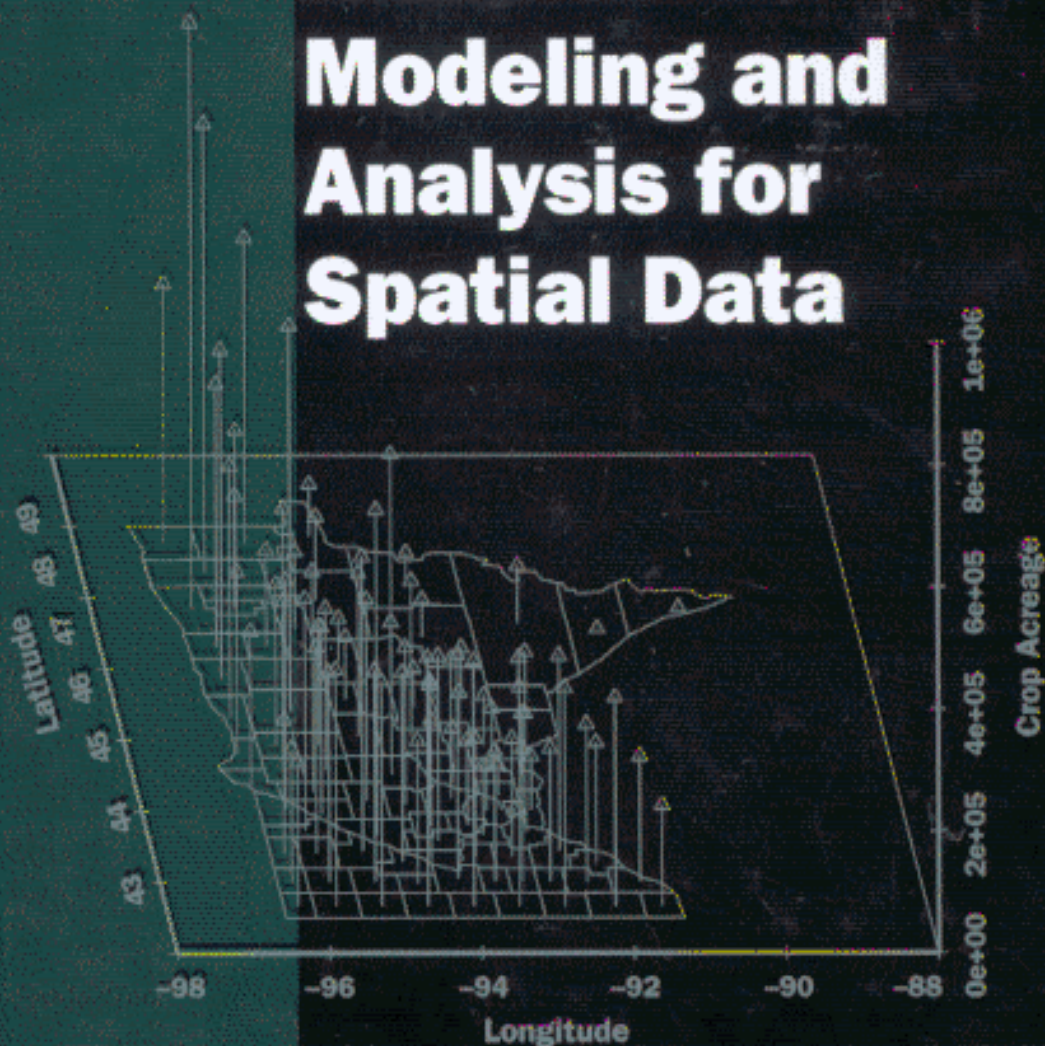


Monographs on Statistics and Applied Probability 101

Hierarchical Modeling and Analysis for Spatial Data



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