

# **OFDM** and **MC-CDMA**

**for Broadband Multi-User  
Communications, WLANs  
and Broadcasting**

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# Contents

|                                                                  |               |
|------------------------------------------------------------------|---------------|
| <b>About the Authors</b>                                         | <b>xxix</b>   |
| <b>Other Wiley and IEEE Press Books on Related Topics</b>        | <b>xxxi</b>   |
| <b>Acknowledgments</b>                                           | <b>xxxiii</b> |
| <b>1 Introduction</b>                                            | <b>1</b>      |
| 1.1 Motivation of the Book . . . . .                             | 1             |
| 1.2 Orthogonal Frequency Division Multiplexing History . . . . . | 5             |
| 1.2.1 Early Classic Contributions . . . . .                      | 5             |
| 1.2.2 Peak-to-mean Power Ratio . . . . .                         | 6             |
| 1.2.3 Synchronisation . . . . .                                  | 7             |
| 1.2.4 OFDM/CDMA . . . . .                                        | 7             |
| 1.2.5 Decision-Directed Channel Estimation . . . . .             | 8             |
| 1.2.6 Detection Techniques for Multi-User SDMA-OFDM . . . . .    | 13            |
| 1.2.7 OFDM Applications . . . . .                                | 13            |
| 1.3 Outline of the Book . . . . .                                | 16            |
| 1.4 Chapter Summary and Conclusion . . . . .                     | 19            |
| <b>I OFDM System Design</b>                                      | <b>21</b>     |
| <b>2 Introduction to OFDM</b>                                    | <b>23</b>     |
| 2.1 Introduction . . . . .                                       | 23            |
| 2.2 Principles of QAM-OFDM . . . . .                             | 25            |
| 2.3 Modulation by DFT . . . . .                                  | 27            |
| 2.4 Transmission via Bandlimited Channels . . . . .              | 32            |
| 2.5 Generalised Nyquist Criterion . . . . .                      | 34            |
| 2.6 Basic OFDM Modem Implementations . . . . .                   | 39            |
| 2.7 Cyclic OFDM Symbol Extension . . . . .                       | 41            |
| 2.8 Reducing MDI by Compensation . . . . .                       | 42            |
| 2.8.1 Transient System Analysis . . . . .                        | 42            |

|           |                                                             |           |
|-----------|-------------------------------------------------------------|-----------|
| 2.8.2     | Recursive MDI Compensation . . . . .                        | 44        |
| 2.9       | Decision-Directed Adaptive Channel Equalisation . . . . .   | 46        |
| 2.10      | OFDM Bandwidth Efficiency . . . . .                         | 47        |
| 2.11      | Chapter Summary and Conclusion . . . . .                    | 49        |
| <b>3</b>  | <b>OFDM Transmission over Gaussian Channels</b>             | <b>51</b> |
| 3.1       | Orthogonal Frequency Division Multiplexing . . . . .        | 52        |
| 3.1.1     | History . . . . .                                           | 52        |
| 3.1.1.1   | Peak-to-Mean Power Ratio . . . . .                          | 53        |
| 3.1.1.2   | Synchronisation . . . . .                                   | 53        |
| 3.1.1.3   | OFDM/CDMA . . . . .                                         | 54        |
| 3.1.1.4   | Adaptive Antennas . . . . .                                 | 54        |
| 3.1.1.5   | OFDM Applications . . . . .                                 | 54        |
| 3.2       | Choice of the OFDM Modulation . . . . .                     | 54        |
| 3.3       | OFDM System Performance over AWGN Channels . . . . .        | 55        |
| 3.4       | Clipping Amplification . . . . .                            | 56        |
| 3.4.1     | OFDM Signal Amplitude Statistics . . . . .                  | 56        |
| 3.4.2     | Clipping Amplifier Simulations . . . . .                    | 57        |
| 3.4.2.1   | Introduction to Peak-Power Reduction Techniques . . . . .   | 58        |
| 3.4.2.2   | BER Performance Using Clipping Amplifiers . . . . .         | 59        |
| 3.4.2.3   | Signal Spectrum with Clipping Amplifier . . . . .           | 60        |
| 3.4.3     | Clipping Amplification – Summary . . . . .                  | 62        |
| 3.5       | Analogue-to-Digital Conversion . . . . .                    | 63        |
| 3.6       | Phase Noise . . . . .                                       | 65        |
| 3.6.1     | Effects of Phase Noise . . . . .                            | 66        |
| 3.6.2     | Phase Noise Simulations . . . . .                           | 66        |
| 3.6.2.1   | White Phase Noise Model . . . . .                           | 67        |
| 3.6.2.1.1 | Serial Modem . . . . .                                      | 67        |
| 3.6.2.1.2 | OFDM Modem . . . . .                                        | 67        |
| 3.6.2.2   | Coloured Phase Noise Model . . . . .                        | 70        |
| 3.6.3     | Phase Noise – Summary . . . . .                             | 72        |
| 3.7       | Chapter Summary and Conclusion . . . . .                    | 72        |
| <b>4</b>  | <b>OFDM Transmission over Wideband Channels</b>             | <b>75</b> |
| 4.1       | The Channel Model . . . . .                                 | 75        |
| 4.1.1     | The Wireless Asynchronous Transfer Mode System . . . . .    | 76        |
| 4.1.1.1   | The WATM Channel . . . . .                                  | 76        |
| 4.1.1.2   | The Shortened WATM Channel . . . . .                        | 78        |
| 4.1.2     | The Wireless Local Area Network . . . . .                   | 78        |
| 4.1.2.1   | The WLAN Channel . . . . .                                  | 79        |
| 4.1.3     | UMTS System . . . . .                                       | 79        |
| 4.1.3.1   | The UMTS Type Channel . . . . .                             | 79        |
| 4.2       | Effects of Time Dispersive Channels on OFDM . . . . .       | 80        |
| 4.2.1     | Effects of the Stationary Time Dispersive Channel . . . . . | 81        |
| 4.2.2     | Non-Stationary Channel . . . . .                            | 82        |
| 4.2.2.1   | Summary of Time-variant Channels . . . . .                  | 84        |

|           |                                                                         |            |
|-----------|-------------------------------------------------------------------------|------------|
| 4.2.3     | Signalling over Time-Dispersive OFDM Channels . . . . .                 | 84         |
| 4.3       | Channel Transfer Function Estimation . . . . .                          | 84         |
| 4.3.1     | Frequency Domain Channel Transfer Function Estimation . . . . .         | 85         |
| 4.3.1.1   | Pilot Symbol-Assisted Schemes . . . . .                                 | 85         |
| 4.3.1.1.1 | Linear Interpolation for PSAM . . . . .                                 | 85         |
| 4.3.1.1.2 | Ideal Lowpass Interpolation for PSAM . . . . .                          | 89         |
| 4.3.1.1.3 | Summary . . . . .                                                       | 89         |
| 4.3.2     | Time Domain Channel Estimation . . . . .                                | 92         |
| 4.4       | System Performance . . . . .                                            | 92         |
| 4.4.1     | Static Time-Dispersive Channel . . . . .                                | 92         |
| 4.4.1.1   | Perfect Channel Estimation . . . . .                                    | 93         |
| 4.4.1.2   | Differentially Coded Modulation . . . . .                               | 95         |
| 4.4.1.3   | PSAM Aided Channel Transfer Function Estimation . . . . .               | 98         |
| 4.4.2     | Slowly Varying Time-Dispersive Channel . . . . .                        | 103        |
| 4.4.2.1   | Perfect Channel Estimation . . . . .                                    | 104        |
| 4.4.2.2   | Pilot Symbol Assisted Modulation Summary . . . . .                      | 104        |
| 4.5       | Intersubcarrier Interference Cancellation . . . . .                     | 106        |
| 4.5.1     | Motivation . . . . .                                                    | 106        |
| 4.5.2     | The Signal Model . . . . .                                              | 109        |
| 4.5.3     | Channel Estimation . . . . .                                            | 110        |
| 4.5.4     | Cancellation Schemes . . . . .                                          | 112        |
| 4.5.5     | ICI Cancellation Performance . . . . .                                  | 113        |
| 4.5.6     | Conclusions on ICI Cancellation . . . . .                               | 114        |
| 4.6       | Chapter Summary and Conclusion . . . . .                                | 116        |
| <b>5</b>  | <b>Time and Frequency Domain Synchronisation</b> . . . . .              | <b>117</b> |
| 5.1       | Performance with Frequency and Timing Errors . . . . .                  | 117        |
| 5.1.1     | Frequency Shift . . . . .                                               | 117        |
| 5.1.1.1   | The Spectrum of the OFDM Signal . . . . .                               | 118        |
| 5.1.1.2   | Effects of Frequency Mismatch on Different Modulation Schemes . . . . . | 122        |
| 5.1.1.2.1 | Coherent Modulation . . . . .                                           | 122        |
| 5.1.1.2.2 | Pilot Symbol Assisted Modulation . . . . .                              | 123        |
| 5.1.1.2.3 | Differential Modulation . . . . .                                       | 123        |
| 5.1.1.2.4 | Frequency Error - Summary . . . . .                                     | 123        |
| 5.1.2     | Time Domain Synchronisation Errors . . . . .                            | 124        |
| 5.1.2.1   | Coherent Demodulation . . . . .                                         | 125        |
| 5.1.2.2   | Pilot Symbol-Assisted Modulation . . . . .                              | 125        |
| 5.1.2.3   | Differential Modulation . . . . .                                       | 126        |
| 5.1.2.3.1 | Time Domain Synchronisation Errors - Summary . . . . .                  | 128        |
| 5.2       | Synchronisation Algorithms . . . . .                                    | 129        |
| 5.2.1     | Coarse Frame and OFDM Symbol Synchronisation Review . . . . .           | 130        |
| 5.2.2     | Fine Symbol Tracking Review . . . . .                                   | 130        |
| 5.2.3     | Frequency Acquisition Review . . . . .                                  | 130        |
| 5.2.4     | Frequency Tracking Review . . . . .                                     | 131        |
| 5.2.5     | Synchronisation by Auto-correlation . . . . .                           | 131        |

|           |                                                                         |            |
|-----------|-------------------------------------------------------------------------|------------|
| 5.2.6     | Multiple Access Frame Structure                                         | 131        |
| 5.2.6.1   | The Reference Symbol                                                    | 132        |
| 5.2.6.2   | The Correlation Functions                                               | 133        |
| 5.2.7     | Frequency Tracking and OFDM Symbol Synchronisation                      | 134        |
| 5.2.7.1   | OFDM Symbol Synchronisation                                             | 134        |
| 5.2.7.2   | Frequency Tracking Studies                                              | 134        |
| 5.2.8     | Frequency Acquisition and Frame Synchronisation Studies                 | 136        |
| 5.2.8.1   | Frame Synchronisation Studies                                           | 136        |
| 5.2.8.2   | Frequency Acquisition Studies                                           | 136        |
| 5.2.8.3   | Block Diagram of the Synchronisation Algorithms                         | 137        |
| 5.2.9     | Synchronisation Using Pilots                                            | 138        |
| 5.2.9.1   | The Reference Symbol                                                    | 138        |
| 5.2.9.2   | Frequency Acquisition                                                   | 138        |
| 5.2.9.3   | Performance of the Pilot-Based Frequency Acquisition in AWGN Channels   | 141        |
| 5.2.9.4   | Alternative Frequency Error Estimation for Frequency Domain Pilot Tones | 145        |
| 5.3       | Comparison of the Frequency Acquisition Algorithms                      | 147        |
| 5.4       | BER Performance with Frequency Synchronisation                          | 151        |
| 5.5       | Chapter Summary and Conclusion                                          | 152        |
| 5.6       | Appendix: OFDM Synchronisation Performance                              | 153        |
| 5.6.1     | Frequency Synchronisation in an AWGN Channel                            | 153        |
| 5.6.1.1   | One Phasor in AWGN Environment                                          | 153        |
| 5.6.1.1.1 | Cartesian Coordinates                                                   | 153        |
| 5.6.1.1.2 | Polar Coordinates                                                       | 153        |
| 5.6.1.2   | Product of Two Noisy Phasors                                            | 154        |
| 5.6.1.2.1 | Joint Probability Density                                               | 154        |
| 5.6.1.2.2 | Phase Distribution                                                      | 155        |
| 5.6.1.2.3 | Numerical Integration                                                   | 155        |
| <b>6</b>  | <b>Adaptive Single- and Multi-user OFDM</b>                             | <b>159</b> |
| 6.1       | Introduction                                                            | 159        |
| 6.1.1     | Motivation                                                              | 159        |
| 6.1.2     | Adaptive Techniques                                                     | 160        |
| 6.1.2.1   | Channel Quality Estimation                                              | 161        |
| 6.1.2.2   | Parameter Adaptation                                                    | 162        |
| 6.1.2.3   | Signalling the AOFDM Parameters                                         | 162        |
| 6.1.3     | System Aspects                                                          | 164        |
| 6.2       | Adaptive Modulation for OFDM                                            | 164        |
| 6.2.1     | System Model                                                            | 164        |
| 6.2.2     | Channel Model                                                           | 165        |
| 6.2.3     | Channel Transfer Function Variations                                    | 166        |
| 6.2.4     | Choice of the Modulation Modes                                          | 166        |
| 6.2.4.1   | Fixed Threshold Adaptation Algorithm                                    | 167        |
| 6.2.4.2   | Sub-band BER Estimator Adaptation Algorithm                             | 169        |
| 6.2.5     | Constant Throughput Adaptive OFDM                                       | 170        |

|         |                                                           |     |
|---------|-----------------------------------------------------------|-----|
| 6.2.6   | AOFD Mode Signalling and Blind Detection . . . . .        | 172 |
| 6.2.6.1 | Signalling . . . . .                                      | 172 |
| 6.2.6.2 | Blind Detection by SNR Estimation . . . . .               | 174 |
| 6.2.6.3 | Blind Detection by Multi-Mode Trellis Decoder . . . . .   | 175 |
| 6.2.7   | Sub-band Adaptive OFDM and Turbo Channel Coding . . . . . | 177 |
| 6.2.8   | Effects of the Doppler Frequency . . . . .                | 179 |
| 6.2.9   | Channel Transfer Function Estimation . . . . .            | 179 |
| 6.3     | Adaptive OFDM Speech System . . . . .                     | 183 |
| 6.3.1   | Introduction . . . . .                                    | 183 |
| 6.3.2   | System Overview . . . . .                                 | 183 |
| 6.3.2.1 | System Parameters . . . . .                               | 184 |
| 6.3.3   | Constant Throughput Adaptive Modulation . . . . .         | 185 |
| 6.3.3.1 | Constant-Rate BER Performance . . . . .                   | 186 |
| 6.3.4   | Multimode Adaptation . . . . .                            | 188 |
| 6.3.4.1 | Mode Switching . . . . .                                  | 188 |
| 6.3.5   | Simulation Results . . . . .                              | 189 |
| 6.3.5.1 | Frame Error Results . . . . .                             | 189 |
| 6.3.5.2 | Audio Segmental SNR . . . . .                             | 190 |
| 6.4     | Pre-equalisation . . . . .                                | 191 |
| 6.4.1   | Motivation . . . . .                                      | 191 |
| 6.4.2   | Pre-equalisation with Sub-band Blocking . . . . .         | 195 |
| 6.4.3   | Adaptive Modulation with Spectral Predistortion . . . . . | 196 |
| 6.5     | Comparison of the Adaptive Techniques . . . . .           | 199 |
| 6.6     | Near-optimum Power- and Bit-allocation in OFDM . . . . .  | 201 |
| 6.6.1   | State of the Art . . . . .                                | 201 |
| 6.6.2   | Problem Description . . . . .                             | 201 |
| 6.6.3   | Power and Bit Allocation Algorithm . . . . .              | 202 |
| 6.7     | Multi-User AOFDM . . . . .                                | 205 |
| 6.7.1   | Introduction . . . . .                                    | 206 |
| 6.7.2   | Adaptive Transceiver Architecture . . . . .               | 206 |
| 6.7.2.1 | An Overview . . . . .                                     | 206 |
| 6.7.2.2 | The Signal Model . . . . .                                | 207 |
| 6.7.2.3 | The SMI Algorithm . . . . .                               | 208 |
| 6.7.2.4 | The Adaptive Bit-assignment Algorithm - . . . . .         | 209 |
| 6.7.2.5 | The Channel Models . . . . .                              | 209 |
| 6.7.3   | Simulation Results - Perfect Channel Knowledge . . . . .  | 210 |
| 6.7.3.1 | General Remarks . . . . .                                 | 210 |
| 6.7.3.2 | Two-Branch Maximum-Ratio Combining . . . . .              | 210 |
| 6.7.3.3 | SMI Co-Channel Interference Suppression . . . . .         | 210 |
| 6.7.4   | Pilot-based Channel Parameter Estimation . . . . .        | 215 |
| 6.7.4.1 | System Description . . . . .                              | 215 |
| 6.7.4.2 | Simulation Results - . . . . .                            | 215 |
| 6.8     | Chapter Summary and Conclusion . . . . .                  | 216 |

|           |                                                                                     |            |
|-----------|-------------------------------------------------------------------------------------|------------|
| <b>7</b>  | <b>Block-Coded Adaptive OFDM</b>                                                    | <b>219</b> |
| 7.1       | Introduction                                                                        | 219        |
| 7.1.1     | Motivation                                                                          | 219        |
| 7.1.2     | Choice of Error Correction Codes                                                    | 220        |
| 7.2       | Redundant Residue Number System Codes                                               | 220        |
| 7.2.1     | Performance in an AWGN channel                                                      | 222        |
| 7.2.1.1   | Performance in a fading time dispersive channel                                     | 223        |
| 7.2.1.2   | Adaptive RRNS-coded OFDM                                                            | 223        |
| 7.2.2     | ARRNS/AOFDM Transceivers                                                            | 229        |
| 7.2.3     | Soft Decision RRNS Decoding                                                         | 231        |
| 7.3       | Turbo BCH Codes                                                                     | 231        |
| 7.3.1     | Adaptive TBCH Coding                                                                | 233        |
| 7.3.2     | Joint ATBCH/AOFDM Algorithm                                                         | 234        |
| 7.4       | Signalling                                                                          | 235        |
| 7.5       | Chapter Summary and Conclusion                                                      | 236        |
| <br>      |                                                                                     |            |
| <b>II</b> | <b>OFDM versus MC-CDMA Systems, Their Spreading Codes and Peak Factor Reduction</b> | <b>239</b> |
| <br>      |                                                                                     |            |
| <b>8</b>  | <b>OFDM versus MC-CDMA</b>                                                          | <b>241</b> |
| 8.1       | Amalgamating DS-CDMA and OFDM                                                       | 241        |
| 8.1.1     | The DS-CDMA Component                                                               | 241        |
| 8.1.2     | The OFDM Component                                                                  | 244        |
| 8.2       | Multi-Carrier CDMA                                                                  | 247        |
| 8.2.1     | MC-CDMA                                                                             | 247        |
| 8.2.2     | MC-DS-CDMA                                                                          | 250        |
| 8.2.3     | MT-CDMA                                                                             | 252        |
| 8.3       | Further Research Topics in MC-CDMA                                                  | 252        |
| 8.4       | Chapter Summary and Conclusion                                                      | 253        |
| <br>      |                                                                                     |            |
| <b>9</b>  | <b>Basic Spreading Sequences</b>                                                    | <b>255</b> |
| 9.1       | PN Sequences                                                                        | 255        |
| 9.1.1     | Maximal Length Sequences                                                            | 255        |
| 9.1.2     | Gold Codes                                                                          | 257        |
| 9.1.3     | Kasami Sequences                                                                    | 258        |
| 9.2       | Orthogonal Codes                                                                    | 259        |
| 9.2.1     | Walsh Codes                                                                         | 259        |
| 9.2.2     | Orthogonal Gold Codes                                                               | 260        |
| 9.2.3     | Multi-rate Orthogonal Gold Codes                                                    | 262        |
| 9.3       | Chapter Summary and Conclusion                                                      | 265        |
| <br>      |                                                                                     |            |
| <b>10</b> | <b>MC-CDMA Performance in Synchronous Environments</b>                              | <b>267</b> |
| 10.1      | The Frequency Selective Channel Model                                               | 268        |
| 10.2      | The System Model                                                                    | 270        |
| 10.3      | Single User Detection                                                               | 271        |
| 10.3.1    | Maximal Ratio Combining                                                             | 272        |

|           |                                                                             |            |
|-----------|-----------------------------------------------------------------------------|------------|
| 10.3.2    | Equal Gain Combining . . . . .                                              | 276        |
| 10.3.3    | Orthogonality Restoring Combining . . . . .                                 | 278        |
| 10.4      | Multi-User Detection . . . . .                                              | 279        |
| 10.4.1    | Maximum Likelihood Detection . . . . .                                      | 280        |
| 10.5      | Chapter Summary and Conclusion . . . . .                                    | 281        |
| <b>11</b> | <b>Advanced Peak Factor Reduction Techniques</b>                            | <b>283</b> |
| 11.1      | Introduction . . . . .                                                      | 283        |
| 11.2      | Measures of Peakiness . . . . .                                             | 285        |
| 11.3      | Special Sequences for Reducing Amplitude Variations . . . . .               | 286        |
| 11.3.1    | Shapiro-Rudin Sequences . . . . .                                           | 286        |
| 11.3.2    | Golay Codes . . . . .                                                       | 288        |
| 11.3.3    | M-Sequences . . . . .                                                       | 289        |
| 11.3.4    | Newman Phases and Schroeder Phases . . . . .                                | 290        |
| 11.3.5    | Barker Codes . . . . .                                                      | 293        |
| 11.3.6    | Comparison of Various Schemes . . . . .                                     | 294        |
| 11.4      | Crest Factor Reduction Mapping Schemes for OFDM . . . . .                   | 295        |
| 11.4.1    | Some Properties of the Peak Factors in OFDM . . . . .                       | 295        |
| 11.4.2    | CF-Reduction Block Coding Scheme . . . . .                                  | 297        |
| 11.4.3    | Selected Mapping-Based CF-Reduction . . . . .                               | 299        |
| 11.4.4    | Partial Transmit Sequences . . . . .                                        | 300        |
| 11.5      | Peak Factors in Multi-Carrier CDMA . . . . .                                | 300        |
| 11.5.1    | System Model and Envelope Power . . . . .                                   | 301        |
| 11.5.2    | Spreading Sequences and Crest Factors . . . . .                             | 306        |
| 11.5.2.1  | Single-code Signal . . . . .                                                | 306        |
| 11.5.2.2  | Shapiro-Rudin-based Spreading Sequences . . . . .                           | 311        |
| 11.5.2.3  | Peak Factor Distribution of Multi-Code MC-CDMA . . . . .                    | 320        |
| 11.5.3    | Clipping Amplifier and BER Comparison . . . . .                             | 323        |
| 11.5.3.1  | Non-linear Power Amplifier Model . . . . .                                  | 323        |
| 11.5.3.2  | Clipping Effects on Output Power . . . . .                                  | 325        |
| 11.5.3.3  | Effects of Clipping on the Bit Error Ratio . . . . .                        | 327        |
| 11.5.3.4  | Clipping Effects on Frequency Spectrum . . . . .                            | 332        |
| 11.5.4    | Diversity Considerations . . . . .                                          | 334        |
| 11.6      | Chapter Summary and Conclusion . . . . .                                    | 335        |
| 11.7      | Appendix: Peak-to-mean Envelope Power Ratio of OFDM Systems . . . . .       | 336        |
| 11.7.1    | PMEPR Analysis of BPSK Modulated OFDM . . . . .                             | 336        |
| 11.7.2    | PMEPR Properties of BPSK Modulated OFDM . . . . .                           | 337        |
| 11.7.3    | PMEPR Calculation of BPSK Modulated OFDM . . . . .                          | 348        |
| 11.7.4    | PMEPR Properties of QPSK Modulated OFDM . . . . .                           | 349        |
| <b>12</b> | <b>Adaptive Modulation for OFDM and MC-CDMA</b>                             | <b>353</b> |
| 12.1      | Introduction . . . . .                                                      | 353        |
| 12.2      | Increasing the Average Transmit Power as a Fading Counter-Measure . . . . . | 354        |
| 12.3      | System Description . . . . .                                                | 358        |
| 12.3.1    | General Model . . . . .                                                     | 359        |
| 12.3.2    | Examples . . . . .                                                          | 359        |

|          |                                                                                                                         |            |
|----------|-------------------------------------------------------------------------------------------------------------------------|------------|
| 12.3.2.1 | Five-Mode AQAM . . . . .                                                                                                | 359        |
| 12.3.2.2 | Seven-Mode Adaptive Star-QAM . . . . .                                                                                  | 360        |
| 12.3.2.3 | Five-Mode APSK . . . . .                                                                                                | 360        |
| 12.3.2.4 | Ten-Mode AQAM . . . . .                                                                                                 | 361        |
| 12.3.3   | Characteristic Parameters . . . . .                                                                                     | 361        |
| 12.3.3.1 | Closed Form Expressions for Transmission over Nakagami<br>Fading Channels . . . . .                                     | 363        |
| 12.4     | Optimum Switching Levels . . . . .                                                                                      | 365        |
| 12.4.1   | Limiting the Peak Instantaneous BEP . . . . .                                                                           | 366        |
| 12.4.2   | Torrance's Switching Levels . . . . .                                                                                   | 369        |
| 12.4.3   | Cost Function Optimisation as a Function of the Average SNR . . . . .                                                   | 371        |
| 12.4.4   | Lagrangian Method . . . . .                                                                                             | 374        |
| 12.5     | Results and Discussion . . . . .                                                                                        | 384        |
| 12.5.1   | Narrow-band Nakagami- $m$ Fading Channel . . . . .                                                                      | 385        |
| 12.5.1.1 | Adaptive PSK Modulation Schemes . . . . .                                                                               | 385        |
| 12.5.1.2 | Adaptive Coherent Star QAM Schemes . . . . .                                                                            | 391        |
| 12.5.1.3 | Adaptive Coherent Square QAM Modulation Schemes . . . . .                                                               | 398        |
| 12.5.2   | Performance over Narrow-band Rayleigh Channels Using Antenna<br>Diversity . . . . .                                     | 402        |
| 12.5.3   | Performance over Wideband Rayleigh Channels using Antenna Di-<br>versity . . . . .                                      | 405        |
| 12.5.4   | Uncoded Adaptive Multi-Carrier Schemes . . . . .                                                                        | 408        |
| 12.5.5   | Concatenated Space-Time Block Coded and Turbo Coded Symbol-<br>by-Symbol Adaptive OFDM and Multi-Carrier CDMA . . . . . | 411        |
| 12.6     | Chapter Summary and Conclusion . . . . .                                                                                | 416        |
| 12.7     | Appendix: Mode Specific Average BEP of Adaptive Modulation . . . . .                                                    | 417        |
| 12.8     | Appendix: BER Analysis of Type-I Star-QAM . . . . .                                                                     | 419        |
| 12.8.1   | Coherent Detection . . . . .                                                                                            | 419        |
| 12.9     | Appendix: Two-Dimensional Rake Receiver . . . . .                                                                       | 429        |
| 12.9.1   | System Model . . . . .                                                                                                  | 429        |
| 12.9.2   | BER Analysis of Fixed-mode Square QAM . . . . .                                                                         | 431        |
| 13       | <b>Successive Partial Despreading Based Multi-Code MC-CDMA</b> . . . . .                                                | <b>437</b> |
| 13.1     | Introduction . . . . .                                                                                                  | 437        |
| 13.2     | System Model . . . . .                                                                                                  | 438        |
| 13.3     | The Sequential Partial Despreading Concept . . . . .                                                                    | 440        |
| 13.4     | AWGN Channel . . . . .                                                                                                  | 443        |
| 13.4.1   | Type I Detector . . . . .                                                                                               | 444        |
| 13.4.2   | Type II Detector . . . . .                                                                                              | 444        |
| 13.4.3   | Type III Detector . . . . .                                                                                             | 450        |
| 13.4.4   | Summary and Discussion . . . . .                                                                                        | 455        |
| 13.5     | Effects of Impulse Noise or Narrow Band Jamming . . . . .                                                               | 457        |
| 13.5.1   | Conventional BPSK System without Spreading . . . . .                                                                    | 457        |
| 13.5.2   | Conventional Despreading Scheme . . . . .                                                                               | 457        |
| 13.5.3   | SPD Detectors . . . . .                                                                                                 | 461        |
| 13.5.4   | Type I Detector . . . . .                                                                                               | 464        |

|                                               |     |
|-----------------------------------------------|-----|
| 13.5.5 Type II Detector . . . . .             | 468 |
| 13.5.6 Type III Detector . . . . .            | 471 |
| 13.5.7 Summary and Discussion . . . . .       | 476 |
| 13.6 Chapter Summary and Conclusion . . . . . | 477 |

### III Advanced Topics: Channel Estimation and Multi-user OFDM Systems 479

#### List of General Symbols 481

|                                                                                                                                                                                 |            |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------|
| <b>14 Pilot-Assisted Channel Estimation for Single-User OFDM</b> . . . . .                                                                                                      | <b>485</b> |
| 14.1 Introduction . . . . .                                                                                                                                                     | 485        |
| 14.1.1 <i>Classification of Channel Estimation Techniques</i> . . . . .                                                                                                         | 487        |
| 14.2 The Stochastic Channel Model . . . . .                                                                                                                                     | 489        |
| 14.2.1 Model of the Channel Impulse Response . . . . .                                                                                                                          | 490        |
| 14.2.2 Auto-Correlation Function of the CIR: $r_h(\Delta t, \tau)$ . . . . .                                                                                                    | 491        |
| 14.2.3 Spaced-Time Spaced-Frequency Correlation Function - Fourier Transform of the CIR's ACF with Respect to the Multipath Delay Variable: $r_H(\Delta t, \Delta f)$ . . . . . | 491        |
| 14.2.4 Fourier Transform of the CIR's ACF with Respect to the Multipath Delay- and Spaced-Time Variables: $S_H(f_d, \Delta f)$ . . . . .                                        | 492        |
| 14.2.5 Scattering Function - Fourier Transform of the CIR's ACF with Respect to the Time-Delay: $S_h(f_d, \tau)$ . . . . .                                                      | 493        |
| 14.2.6 Separability of the Channel's Spaced-Time Spaced-Frequency Correlation Function . . . . .                                                                                | 493        |
| 14.3 Channel Model for Monte Carlo Simulations . . . . .                                                                                                                        | 495        |
| 14.3.1 The Indoor WATM Model . . . . .                                                                                                                                          | 495        |
| 14.4 Introduction to 2D-Signal Processing . . . . .                                                                                                                             | 496        |
| 14.4.1 Description of a 2D-Sequence by a Periodicity Matrix . . . . .                                                                                                           | 496        |
| 14.5 <i>Maximum Pilot-Distances for a Rectangular Pilot Grid</i> . . . . .                                                                                                      | 498        |
| 14.5.1 Sampling in the Frequency Direction . . . . .                                                                                                                            | 498        |
| 14.5.2 Sampling in the Time Direction . . . . .                                                                                                                                 | 499        |
| 14.6 2D-Pilot Pattern-Assisted 2D-FIR Wiener Filter-Aided Channel Estimation . . . . .                                                                                          | 500        |
| 14.6.1 Derivation of the Optimum Estimator Coefficients and Estimator MSE for Matched and Mismatched Channel Statistics . . . . .                                               | 500        |
| 14.6.1.1 Linear Channel Transfer Factor Estimate . . . . .                                                                                                                      | 501        |
| 14.6.1.2 Estimator MSE and Cost-Function . . . . .                                                                                                                              | 503        |
| 14.6.1.3 Optimum Estimator Coefficients and Minimum Estimator MSE . . . . .                                                                                                     | 504        |
| 14.6.1.4 Estimator Coefficients for Mismatched Channel Statistics . . . . .                                                                                                     | 505        |
| 14.6.2 Robust Estimator Design . . . . .                                                                                                                                        | 505        |
| 14.6.2.1 Uniform Scattering Function and its Associated Spaced-Time Spaced-Frequency Correlation Function . . . . .                                                             | 506        |
| 14.6.2.2 Relevance of the Shift-Parameter . . . . .                                                                                                                             | 507        |
| 14.6.2.3 Application to a Robust Estimator . . . . .                                                                                                                            | 507        |

|            |                                                                                                                                               |     |
|------------|-----------------------------------------------------------------------------------------------------------------------------------------------|-----|
| 14.6.3     | Complexity Reduction . . . . .                                                                                                                | 508 |
| 14.6.3.1   | Number of Pilot Subcarriers in the Estimator's Input Block . . . . .                                                                          | 508 |
| 14.6.3.2   | Selection of Subsets of Pilot Subcarriers . . . . .                                                                                           | 509 |
| 14.6.4     | MSE Performance of 2D-FIR Wiener Filtering . . . . .                                                                                          | 509 |
| 14.6.4.1   | Simulation Parameters - Design of the Pilot Grid and the Uniform Scattering Function used in the Calculation of Filter Coefficients . . . . . | 510 |
| 14.6.4.2   | Evolution of the Estimator MSE over a Period of the Rectangular Pilot Grid . . . . .                                                          | 512 |
| 14.6.4.3   | Influence of the Pilot Grid Density and the Number of Filter Taps on the Estimator's MSE . . . . .                                            | 513 |
| 14.6.5     | Computational Complexity . . . . .                                                                                                            | 514 |
| 14.6.6     | Summary and Conclusion on 2D-FIR Wiener Filtering . . . . .                                                                                   | 515 |
| 14.7       | Cascaded 1D-FIR Wiener filtering . . . . .                                                                                                    | 516 |
| 14.7.1     | Derivation of the Optimum Estimator Coefficients and Estimator MSE for both Matched and Mismatched Channel Statistics . . . . .               | 517 |
| 14.7.1.1   | First-Stage Channel Estimates - Interpolation in the Frequency Direction . . . . .                                                            | 517 |
| 14.7.1.1.1 | Linear Channel Transfer Factor Estimate . . . . .                                                                                             | 517 |
| 14.7.1.1.2 | Estimator Coefficients for Mismatched Channel Statistics . . . . .                                                                            | 518 |
| 14.7.1.1.3 | Estimator MSE . . . . .                                                                                                                       | 518 |
| 14.7.1.2   | Second-Stage Channel Estimates - Interpolation in the Time Direction . . . . .                                                                | 519 |
| 14.7.1.2.1 | Linear Channel Transfer Factor Estimate . . . . .                                                                                             | 519 |
| 14.7.1.2.2 | Estimator Coefficients for Mismatched Channel Statistics . . . . .                                                                            | 520 |
| 14.7.1.2.3 | Estimator MSE . . . . .                                                                                                                       | 521 |
| 14.7.1.3   | Simplification of the Cascaded 1D-FIR Wiener Filter . . . . .                                                                                 | 522 |
| 14.7.2     | MSE Performance of the Cascaded 1D-FIR Wiener Filter . . . . .                                                                                | 522 |
| 14.7.2.1   | Comparison to 2D-FIR Wiener Filtering . . . . .                                                                                               | 523 |
| 14.7.2.2   | Misadjustment of Multipath- and Doppler Spread . . . . .                                                                                      | 525 |
| 14.7.2.3   | Misadjustment of the SNR . . . . .                                                                                                            | 526 |
| 14.7.2.4   | Impact of Imperfect Synchronization . . . . .                                                                                                 | 528 |
| 14.7.2.5   | Mismatch of the Multipath Intensity Profile's Shape . . . . .                                                                                 | 532 |
| 14.7.3     | MSE and BER Performance Evaluation by Monte Carlo Simulations . . . . .                                                                       | 535 |
| 14.7.3.1   | Simulation Parameters . . . . .                                                                                                               | 536 |
| 14.7.3.2   | MSE Simulation Results . . . . .                                                                                                              | 538 |
| 14.7.3.3   | BER Simulation Results . . . . .                                                                                                              | 539 |
| 14.7.4     | Complexity . . . . .                                                                                                                          | 540 |
| 14.7.4.1   | Computational Complexity . . . . .                                                                                                            | 540 |
| 14.7.4.2   | Number of Coefficient Vectors per SNR Level for Decoupled Cascaded 1D-FIR Filters . . . . .                                                   | 541 |
| 14.7.5     | Summary and Conclusion on Cascaded 1D-FIR Wiener Filtering . . . . .                                                                          | 542 |
| 14.8       | Chapter Summary and Conclusion . . . . .                                                                                                      | 544 |

|                                                                                                                                               |            |
|-----------------------------------------------------------------------------------------------------------------------------------------------|------------|
| 14.9 List of Symbols Used in Chapter 14 . . . . .                                                                                             | 545        |
| <b>15 Decision-Directed Channel Estimation for Single-User OFDM</b> . . . . .                                                                 | <b>549</b> |
| 15.1 Introduction . . . . .                                                                                                                   | 549        |
| 15.2 Description . . . . .                                                                                                                    | 552        |
| 15.2.1 Decision-Directed <i>A Posteriori</i> Least-Squares Channel Estimation . . . . .                                                       | 553        |
| 15.2.2 Enhancement of the <i>A Posteriori</i> Least-Squares Channel Transfer<br>Factor Estimates by One-Dimensional MMSE Estimation . . . . . | 555        |
| 15.2.2.1 Structure of the 1D-MMSE Channel Estimator . . . . .                                                                                 | 555        |
| 15.2.2.2 Estimator MSE for Mismatched Channel Conditions . . . . .                                                                            | 557        |
| 15.2.3 Enhancement of the <i>A Posteriori</i> Least-Squares Channel Transfer<br>Factor Estimates by Two-Dimensional MMSE Estimation . . . . . | 557        |
| 15.2.3.1 Structure of the 2D-MMSE Estimator . . . . .                                                                                         | 558        |
| 15.2.3.2 Estimator MSE for Mismatched Channel Statistics . . . . .                                                                            | 558        |
| 15.2.3.3 Motivation of Time Direction Channel Prediction Filtering . . . . .                                                                  | 561        |
| 15.2.4 MMSE <i>A Priori</i> Time Direction Channel Prediction Filtering . . . . .                                                             | 563        |
| 15.2.4.1 Linear Prediction of the CIR-Related Taps . . . . .                                                                                  | 564        |
| 15.2.4.2 Auto-Correlation Matrix and Cross-Correlation Vector of<br>the CIR . . . . .                                                         | 565        |
| 15.2.4.3 Derivation of the Wiener Equation using the Gradient Ap-<br>proach . . . . .                                                         | 566        |
| 15.2.4.3.1 Gradient Approach . . . . .                                                                                                        | 566        |
| 15.2.4.3.2 Orthogonality Principle . . . . .                                                                                                  | 567        |
| 15.2.4.4 Optimum Predictor Coefficients and Minimum CIR-Related<br>Domain Predictor MSE . . . . .                                             | 567        |
| 15.2.4.5 Optimum Predictor Coefficients for Mismatched Channel<br>Statistics . . . . .                                                        | 568        |
| 15.2.4.6 Average Channel Predictor MSE in the Frequency Domain . . . . .                                                                      | 569        |
| 15.2.5 Channel Statistics for <i>A Priori</i> Time Direction Channel Prediction<br>Filtering . . . . .                                        | 570        |
| 15.2.5.1 Robust <i>A Priori</i> Time Direction Channel Prediction Filtering . . . . .                                                         | 571        |
| 15.2.5.1.1 Review of Robust Channel Estimation . . . . .                                                                                      | 571        |
| 15.2.5.1.2 Design of the Auto-Correlation Matrix and<br>Cross-Correlation Vector of a Robust Channel<br>Predictor . . . . .                   | 571        |
| 15.2.5.2 Adaptive <i>A Priori</i> Time Direction Channel Prediction Fil-<br>tering . . . . .                                                  | 572        |
| 15.3 Performance of Decision-Directed Channel Prediction Aided-OFDM . . . . .                                                                 | 573        |
| 15.3.1 MSE Performance of a Robust Decision-Directed Channel Predictor<br>in the Context of Error-Free Symbol Decisions . . . . .             | 574        |
| 15.3.1.1 MSE Performance under Matched Channel Conditions . . . . .                                                                           | 575        |
| 15.3.1.2 MSE Performance under Mismatched Channel Conditions<br>with Respect to the Doppler Frequency . . . . .                               | 575        |
| 15.3.1.3 MSE Performance under Mismatched Channel SNR Con-<br>ditions . . . . .                                                               | 579        |

|          |                                                                                                                                          |     |
|----------|------------------------------------------------------------------------------------------------------------------------------------------|-----|
| 15.3.1.4 | MSE Performance under Mismatched Multipath Spread Conditions . . . . .                                                                   | 580 |
| 15.3.1.5 | Conclusion on the MSE Performance of Robust Decision-Directed Channel Prediction in the Context of Error-Free Symbol Decisions . . . . . | 581 |
| 15.3.2   | MSE Performance of an Adaptive Decision-Directed Channel Predictor in the Context of Error-Free Symbol Decisions . . . . .               | 581 |
| 15.3.2.1 | MSE Performance under Matched Channel Conditions as a Function of the Number of Samples invoked in the Predictor Design . . . . .        | 582 |
| 15.3.2.2 | MSE Performance in Comparison to that of the Robust Channel Transfer Function Predictor . . . . .                                        | 584 |
| 15.3.2.3 | MSE Performance for Various Multipath Intensity Profiles . . . . .                                                                       | 585 |
| 15.3.2.4 | Conclusion on Adaptive Decision-Directed Channel Prediction in the Context of Error-Free Symbol Decisions . . . . .                      | 586 |
| 15.3.3   | MSE Performance of a Robust Decision-Directed Channel Predictor in the Context of an Uncoded System . . . . .                            | 587 |
| 15.3.3.1 | MSE Performance for a Frame-Invariant Fading Channel and for Error-Free Symbol Decisions . . . . .                                       | 589 |
| 15.3.3.2 | MSE Performance for a Frame-Invariant Fading Channel and Sliced Symbol Decisions . . . . .                                               | 590 |
| 15.3.3.3 | MSE Performance for a Frame-Variant Fading Channel and for Sliced Symbol Decisions . . . . .                                             | 590 |
| 15.3.3.4 | Conclusion on the MSE Performance of a Robust Decision-Directed Channel Predictor . . . . .                                              | 591 |
| 15.3.4   | BER Performance of an Uncoded System Employing Robust Decision-Directed Channel Prediction . . . . .                                     | 592 |
| 15.3.4.1 | BER Performance for BPSK and QPSK . . . . .                                                                                              | 592 |
| 15.3.4.2 | BER Performance for 16QAM . . . . .                                                                                                      | 592 |
| 15.3.4.3 | Conclusion on the BER Performance of an Uncoded System employing Robust Decision-Directed Channel Prediction . . . . .                   | 595 |
| 15.3.5   | BER Performance of a Turbo-Coded System Employing Robust Decision-Directed Channel Prediction . . . . .                                  | 595 |
| 15.3.5.1 | Influence of the ICI Variance on the Subcarrier SNR . . . . .                                                                            | 596 |
| 15.3.5.2 | BER Performance for BPSK Modulation in the Context of an Undecoded Reference . . . . .                                                   | 596 |
| 15.3.5.3 | BER Performance for QPSK Modulation and 16QAM in the Context of an Undecoded Reference . . . . .                                         | 598 |
| 15.3.5.4 | BER Performance for QPSK Modulation in the Context of a Decoded Reference . . . . .                                                      | 600 |
| 15.3.5.5 | Conclusion on the BER Performance of a Turbo-Coded System Employing Robust Decision-Directed Channel Prediction . . . . .                | 601 |
| 15.4     | Robust Decision-Directed Channel Prediction-Assisted Adaptive OFDM . . . . .                                                             | 602 |
| 15.4.1   | Transceiver Structure . . . . .                                                                                                          | 603 |
| 15.4.1.1 | Modulation Mode Adaptation . . . . .                                                                                                     | 604 |

|            |                                                                                                                |            |
|------------|----------------------------------------------------------------------------------------------------------------|------------|
| 15.4.2     | BER Performance                                                                                                | 605        |
| 15.4.2.1   | Motivation of Channel Transfer Function Prediction-Assisted AOFDM                                              | 605        |
| 15.4.2.2   | BER Performance of the Uncoded System                                                                          | 607        |
| 15.4.2.3   | BER Performance of the Turbo-Coded System                                                                      | 609        |
| 15.4.3     | Conclusion on Robust Decision-Directed Channel Prediction Assisted AOFDM                                       | 610        |
| 15.5       | Chapter Summary and Conclusion                                                                                 | 611        |
| 15.5.1     | Description                                                                                                    | 611        |
| 15.5.2     | Performance Assessment                                                                                         | 612        |
| 15.5.3     | Adaptive OFDM Transceiver                                                                                      | 613        |
| 15.6       | List of Symbols Used in Chapter 15                                                                             | 614        |
| <b>16</b>  | <b>Channel Estimation for Multi-User OFDM</b>                                                                  | <b>619</b> |
| 16.1       | Motivation                                                                                                     | 619        |
| 16.2       | The SDMA Signal Model on a Subcarrier Basis                                                                    | 622        |
| 16.3       | Multi-User Multiple Reception Antenna Aided OFDM                                                               | 623        |
| 16.4       | Least-Squares Error Decision-Directed Channel Estimation                                                       | 624        |
| 16.4.1     | Derivation of the LS-Estimator                                                                                 | 625        |
| 16.4.1.1   | The SDMA Signal Model on a Receiver Antenna Basis                                                              | 625        |
| 16.4.1.2   | Sub-Space-Based Approach                                                                                       | 626        |
| 16.4.1.2.1 | Low-Rank Approximation of the $i$ -th User's Vector of Different Subcarriers' Channel Transfer Factors         | 626        |
| 16.4.1.2.2 | Determination of the LS-DDCE Coefficients Using the Gradient Approach                                          | 627        |
| 16.4.1.2.3 | Necessary Condition for Identification of the LS-DDCE Coefficients                                             | 630        |
| 16.4.1.2.4 | Implementation by QR Decomposition                                                                             | 630        |
| 16.4.2     | Least-Squares Channel Estimation MSE in the Context of Both Sample-Spaced and Non-Sample-Spaced CIRs           | 631        |
| 16.4.2.1   | Correlation Matrix of the Channel Transfer Factor Estimates                                                    | 631        |
| 16.4.2.2   | Sample-Spaced CIRs                                                                                             | 633        |
| 16.4.2.2.1 | Auto-Correlation Matrix of the Channel Transfer Factor Estimation Errors                                       | 633        |
| 16.4.2.2.2 | Properties of Optimum Training Sequences                                                                       | 634        |
| 16.4.2.2.3 | <i>A Posteriori</i> Estimation MSE Using Optimum Training Sequences                                            | 636        |
| 16.4.2.3   | Non-Sample-Spaced CIRs                                                                                         | 637        |
| 16.4.2.3.1 | Cross-Correlation Matrix of the Channel Transfer Factor Estimates in the Context of Optimum Training Sequences | 637        |
| 16.4.2.3.2 | Auto-Correlation Matrix of the Channel Transfer Factor Estimates in the Context of Optimum Training Sequences  | 638        |

|            |                                                                                                                                                          |     |
|------------|----------------------------------------------------------------------------------------------------------------------------------------------------------|-----|
| 16.4.2.3.3 | Channel Estimation MSE in the Context of Optimum Training Sequences . . . . .                                                                            | 639 |
| 16.4.3     | <i>A Priori</i> Channel Transfer Function Estimation MSE Enhancement by Linear Prediction of the <i>A Posteriori</i> CIR-Related Tap Estimates . . . . . | 640 |
| 16.4.4     | Simplified Approach to LS-Assisted DDCE . . . . .                                                                                                        | 640 |
| 16.4.5     | Complexity Analysis of the Original- and Simplified LS-Assisted DDCE . . . . .                                                                           | 641 |
| 16.4.5.1   | Complexity of the Original LS-Assisted DDCE . . . . .                                                                                                    | 641 |
| 16.4.5.1.1 | Complexity Associated with Assembling Matrix $\mathbf{Q}[n]$ . . . . .                                                                                   | 642 |
| 16.4.5.1.2 | Complexity Associated with Assembling Vector $\mathbf{p}[n]$ . . . . .                                                                                   | 643 |
| 16.4.5.1.3 | Complexity Associated with Solving the LS System Equations for the Vector of CIR-Related Tap Estimates $\hat{\mathbf{h}}_{apt, K_0}[n]$ . . . . .        | 643 |
| 16.4.5.1.4 | Total Complexity . . . . .                                                                                                                               | 643 |
| 16.4.5.2   | Complexity of the Simplified LS-Assisted DDCE . . . . .                                                                                                  | 644 |
| 16.4.6     | Conclusion on the Original and Simplified LS-Assisted DDCE . . . . .                                                                                     | 645 |
| 16.5       | Frequency Domain Parallel Interference Cancellation Aided DDCE . . . . .                                                                                 | 646 |
| 16.5.1     | The Recursive Channel Estimator . . . . .                                                                                                                | 647 |
| 16.5.1.1   | <i>A Priori</i> and <i>A Posteriori</i> Channel Estimates . . . . .                                                                                      | 647 |
| 16.5.1.2   | <i>A Priori</i> Channel Prediction Filtering . . . . .                                                                                                   | 649 |
| 16.5.1.3   | <i>A Priori</i> Channel Estimation MSE . . . . .                                                                                                         | 651 |
| 16.5.1.4   | <i>A Posteriori</i> Channel Estimation MSE . . . . .                                                                                                     | 653 |
| 16.5.1.5   | Stability Analysis of the Recursive Channel Estimator . . . . .                                                                                          | 654 |
| 16.5.1.6   | Iterative Calculation of the CIR-Related Tap Predictor Coefficients . . . . .                                                                            | 656 |
| 16.5.1.6.1 | Simplified Approach for Identical User Statistics . . . . .                                                                                              | 657 |
| 16.5.1.6.2 | Closed Form Solution for Identical User Statistics and One-Tap CIR-Related Tap Prediction Filtering . . . . .                                            | 658 |
| 16.5.1.7   | Channel Statistics . . . . .                                                                                                                             | 659 |
| 16.5.2     | Performance Assessment . . . . .                                                                                                                         | 661 |
| 16.5.2.1   | Evolution of the <i>A Priori</i> Channel Estimation MSE in a Simplified 2-Tap CIR-Related Tap Prediction Scenario . . . . .                              | 661 |
| 16.5.2.2   | <i>A Priori</i> Channel Estimation MSE in the Context of Ideal, Error-Free Symbol Decisions Assuming a Sample-Spaced CIR . . . . .                       | 662 |
| 16.5.2.2.1 | Optimum Recursive versus Sub-Optimum Transversal CIR-Related Tap Predictor Coefficients - One Tap . . . . .                                              | 663 |
| 16.5.2.2.2 | Optimum Recursive- versus Sub-Optimum Transversal CIR-related Tap Predictor Coefficients - Higher Order . . . . .                                        | 664 |

|            |                                                                                                                                                               |     |
|------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------|-----|
| 16.5.2.2.3 | Influence of the Number of Simultaneous Users in the Context of the Optimum Recursive CIR-Related Tap Predictor Coefficients . . . . .                        | 665 |
| 16.5.2.2.4 | Influence of the OFDM Symbol Normalised Doppler Frequency . . . . .                                                                                           | 667 |
| 16.5.2.2.5 | Influence of a Mismatch of the OFDM Symbol Normalised Doppler Frequency . . . . .                                                                             | 668 |
| 16.5.2.2.6 | Performance Comparison to Li's LS-Assisted DDCE . . . . .                                                                                                     | 670 |
| 16.5.2.3   | Effects of a Non-Sample Spaced CIR in the Context of Ideal, Error-Free Symbol Decisions . . . . .                                                             | 671 |
| 16.5.2.3.1 | Sparse Profiles . . . . .                                                                                                                                     | 672 |
| 16.5.2.3.2 | Uniform Profiles . . . . .                                                                                                                                    | 674 |
| 16.5.2.3.3 | Exponential Profiles . . . . .                                                                                                                                | 675 |
| 16.5.2.3.4 | <i>A Priori</i> Channel Estimation MSE for a Non-Sample Spaced CIR . . . . .                                                                                  | 676 |
| 16.5.2.3.5 | <i>A Priori</i> Channel Transfer Factor Estimation MSE for a Non-Sample Spaced CIR on a Sub-carrier Basis . . . . .                                           | 678 |
| 16.5.2.4   | <i>A Priori</i> Channel Estimation MSE and System BER in the Context of Imperfect, Error-Contaminated Symbol Decisions Assuming a Sample-Spaced CIR . . . . . | 680 |
| 16.5.2.4.1 | Effects of Error-Contaminated Symbol Decisions . . . . .                                                                                                      | 680 |
| 16.5.2.4.2 | MSE and BER Performance in an Uncoded Scenario . . . . .                                                                                                      | 681 |
| 16.5.2.4.3 | BER Performance in the Turbo-Coded Scenario . . . . .                                                                                                         | 682 |
| 16.5.3     | Computational Complexity . . . . .                                                                                                                            | 684 |
| 16.5.3.1   | <i>A Posteriori</i> Channel Estimation Complexity . . . . .                                                                                                   | 684 |
| 16.5.3.2   | <i>A Priori</i> Channel Estimation Complexity . . . . .                                                                                                       | 685 |
| 16.5.4     | Summary and Conclusions . . . . .                                                                                                                             | 686 |
| 16.5.4.1   | Summary and Conclusions on the PIC-Assisted DDCE's Structure . . . . .                                                                                        | 687 |
| 16.5.4.2   | Summary and Conclusions on the Performance Assessment of the PIC-Assisted DDCE . . . . .                                                                      | 688 |
| 16.5.4.2.1 | Performance of the PIC-Assisted DDCE in the Context of Sample-Spaced CIRs and Error-Free Symbol Decisions . . . . .                                           | 688 |
| 16.5.4.2.2 | Performance of the PIC-Assisted DDCE in the Context of Non-Sample-Spaced CIRs and Error-Free Symbol Decisions . . . . .                                       | 689 |
| 16.5.4.2.3 | Performance of the PIC-Assisted DDCE in the Context of Sample-Spaced CIRs and Imperfect, Error-Contaminated Symbol Decisions . . . . .                        | 690 |
| 16.5.4.3   | Summary and Conclusions on the PIC-Assisted DDCE's Computational Complexity . . . . .                                                                         | 690 |
| 16.6       | RLS-Adaptive Parallel Interference Cancellation Aided DDCE . . . . .                                                                                          | 691 |

|            |                                                                                                                    |            |
|------------|--------------------------------------------------------------------------------------------------------------------|------------|
| 16.6.1     | Single-User RLS-Adaptive CIR-Related Tap Prediction . . . . .                                                      | 692        |
| 16.6.1.1   | Review of the RLS Algorithm . . . . .                                                                              | 692        |
| 16.6.1.2   | Potential Simplification by Ensemble Averaging . . . . .                                                           | 693        |
| 16.6.1.3   | MSE Performance Assessment . . . . .                                                                               | 694        |
| 16.6.1.4   | Complexity Study . . . . .                                                                                         | 696        |
| 16.6.2     | RLS-Adaptive PIC-Assisted DDCE for Multi-User OFDM . . . . .                                                       | 697        |
| 16.6.2.1   | MSE Performance Assessment . . . . .                                                                               | 697        |
| 16.6.3     | Conclusion . . . . .                                                                                               | 699        |
| 16.7       | Chapter Summary and Conclusion . . . . .                                                                           | 700        |
| 16.8       | List of Symbols Used in Chapter 16 . . . . .                                                                       | 703        |
| <b>17</b>  | <b>Detection Techniques for Multi-User SDMA-OFDM</b>                                                               | <b>715</b> |
| 17.1       | Introduction . . . . .                                                                                             | 715        |
| 17.1.1     | Classification of Smart Antennas . . . . .                                                                         | 715        |
| 17.1.2     | Introduction to Space-Division-Multiple-Access . . . . .                                                           | 719        |
| 17.1.3     | Classification of Multi-User Detection Techniques . . . . .                                                        | 719        |
| 17.1.4     | Outline of Chapter 17 . . . . .                                                                                    | 720        |
| 17.1.5     | SDMA-MIMO Channel Model . . . . .                                                                                  | 722        |
| 17.2       | Linear Detection Techniques . . . . .                                                                              | 723        |
| 17.2.1     | Characterisation of the Linear Combiner's Output Signal . . . . .                                                  | 724        |
| 17.2.1.1   | Description of the Different Signal Components . . . . .                                                           | 725        |
| 17.2.1.2   | Statistical Characterisation . . . . .                                                                             | 725        |
| 17.2.1.3   | Performance Measures . . . . .                                                                                     | 726        |
| 17.2.2     | Least-Squares Error Detector . . . . .                                                                             | 727        |
| 17.2.2.1   | Simplified Model of the Received Signal . . . . .                                                                  | 727        |
| 17.2.2.2   | Least-Squares Error Cost-Function . . . . .                                                                        | 727        |
| 17.2.2.3   | Recovery of the Transmitted Signals by the Gradient Approach . . . . .                                             | 728        |
| 17.2.2.4   | Condition for Identification . . . . .                                                                             | 729        |
| 17.2.2.5   | Squared Estimation Error in the Received Signals' Domain . . . . .                                                 | 729        |
| 17.2.2.6   | Mean-Square Estimation Error in the Transmitted Signals' Domain . . . . .                                          | 730        |
| 17.2.3     | Minimum Mean-Square Error Detector . . . . .                                                                       | 730        |
| 17.2.3.1   | Mean-Square Error Cost-Function . . . . .                                                                          | 731        |
| 17.2.3.2   | Recovery of the Transmitted Signals by the Gradient Approach . . . . .                                             | 732        |
| 17.2.3.2.1 | Right-Inverse Related Form of the MMSE Combiner . . . . .                                                          | 732        |
| 17.2.3.2.2 | Left-Inverse Related Form of the MMSE Combiner . . . . .                                                           | 733        |
| 17.2.3.3   | Mean-Square Estimation Error in the Transmitted Signals' Domain . . . . .                                          | 734        |
| 17.2.3.4   | Optimum Weight Vector in Standard Form . . . . .                                                                   | 734        |
| 17.2.3.5   | Relation between MMSE and MV Combining . . . . .                                                                   | 735        |
| 17.2.4     | Demodulation of the Different Users' Combiner Output Signals . . . . .                                             | 736        |
| 17.2.4.1   | Approximation of a Specific User's Combiner Output Signal as a Sample of a Complex Gaussian Distribution . . . . . | 736        |

|            |                                                                                                                   |     |
|------------|-------------------------------------------------------------------------------------------------------------------|-----|
| 17.2.4.2   | Determination of a Specific User's Transmitted Symbol by Maximising the <i>A Posteriori</i> Probability . . . . . | 737 |
| 17.2.5     | Generation of Soft-Bit Information for Turbo-Decoding . . . . .                                                   | 738 |
| 17.2.5.1   | Simplification by Maximum Approximation . . . . .                                                                 | 740 |
| 17.2.6     | Performance Analysis . . . . .                                                                                    | 740 |
| 17.2.6.1   | MSE and BER Performance Comparison of LS, MMSE and MVDR Detection . . . . .                                       | 741 |
| 17.2.6.2   | SINR Performance of MMSE Detection for Different Numbers of Users and Reception Antennas . . . . .                | 743 |
| 17.2.6.3   | BER Performance of MMSE Detection for Different Numbers of Users and Reception Antennas . . . . .                 | 744 |
| 17.2.6.4   | BER Performance of Turbo-Coded MMSE Detection-Assisted SDMA-OFDM . . . . .                                        | 745 |
| 17.2.7     | Complexity Analysis . . . . .                                                                                     | 746 |
| 17.2.7.1   | LS Combining . . . . .                                                                                            | 746 |
| 17.2.7.1.1 | LS Combining without Generating the Weight Matrix . . . . .                                                       | 746 |
| 17.2.7.1.2 | LS Combining Generating the Weight Matrix . . . . .                                                               | 747 |
| 17.2.7.2   | MMSE Combining . . . . .                                                                                          | 747 |
| 17.2.7.2.1 | Left-Inverse Related Form of MMSE Combining without Generating the Weight Matrix . . . . .                        | 747 |
| 17.2.7.2.2 | Left-Inverse Related Form of MMSE Combining Generating the Weight Matrix . . . . .                                | 748 |
| 17.2.7.3   | Demodulation of the Linear Combiner's Output Signal . . . . .                                                     | 748 |
| 17.2.7.4   | Simplified Complexity Formulae to be Used in the Comparison of the Different Detectors . . . . .                  | 749 |
| 17.2.8     | Conclusion on Linear Detection Techniques . . . . .                                                               | 750 |
| 17.3       | Non-Linear Detection Techniques . . . . .                                                                         | 751 |
| 17.3.1     | SIC Detection . . . . .                                                                                           | 752 |
| 17.3.1.1   | Standard SIC . . . . .                                                                                            | 754 |
| 17.3.1.2   | M-SIC and its Derivatives . . . . .                                                                               | 757 |
| 17.3.1.2.1 | M-SIC . . . . .                                                                                                   | 758 |
| 17.3.1.2.2 | Partial M-SIC . . . . .                                                                                           | 758 |
| 17.3.1.2.3 | Selective-Decision-Insertion Aided M-SIC . . . . .                                                                | 759 |
| 17.3.1.3   | Generation of Soft-Bit Information for Turbo-Decoding . . . . .                                                   | 759 |
| 17.3.1.3.1 | Generation of Rudimentary Soft-Bits . . . . .                                                                     | 759 |
| 17.3.1.3.2 | Generation of Weighted Soft-Bits . . . . .                                                                        | 760 |
| 17.3.1.4   | Performance Analysis . . . . .                                                                                    | 761 |
| 17.3.1.4.1 | BER and SER Performance of Standard SIC and M-SIC for Different Numbers of Users and Receiver Antennas . . . . .  | 763 |
| 17.3.1.4.2 | SER Performance of Standard SIC and M-SIC on a Per-Detection Stage Basis . . . . .                                | 763 |
| 17.3.1.4.3 | SER Performance of Standard SIC and M-SIC on a Per-Detection Stage Basis for an Error-Free Reference . . . . .    | 764 |

|            |                                                                                                                                  |     |
|------------|----------------------------------------------------------------------------------------------------------------------------------|-----|
| 17.3.1.4.4 | Evaluation of the Error-Propagation-Related Event Probabilities . . . . .                                                        | 767 |
| 17.3.1.4.5 | SER Performance of the Partial M-SIC . . . . .                                                                                   | 768 |
| 17.3.1.4.6 | SER Performance of Selective-Decision-Insertion Aided M-SIC . . . . .                                                            | 768 |
| 17.3.1.4.7 | BER Performance of Turbo-Coded SIC Detection-Assisted SDMA-OFDM . . . . .                                                        | 771 |
| 17.3.1.5   | Complexity Analysis . . . . .                                                                                                    | 772 |
| 17.3.1.5.1 | Complexity of Standard SIC . . . . .                                                                                             | 772 |
| 17.3.1.5.2 | Complexity of M-SIC . . . . .                                                                                                    | 775 |
| 17.3.1.5.3 | Complexity of Partial M-SIC . . . . .                                                                                            | 778 |
| 17.3.1.5.4 | Complexity Comparison of the Different SIC Detectors . . . . .                                                                   | 780 |
| 17.3.1.6   | Summary and Conclusions on SIC Detection Techniques . . . . .                                                                    | 781 |
| 17.3.2     | PIC Detection . . . . .                                                                                                          | 784 |
| 17.3.2.1   | Uncoded PIC . . . . .                                                                                                            | 784 |
| 17.3.2.2   | Turbo-Coded PIC . . . . .                                                                                                        | 788 |
| 17.3.2.3   | Performance Analysis . . . . .                                                                                                   | 790 |
| 17.3.2.3.1 | BER Performance of Uncoded PIC Detection-Assisted SDMA-OFDM for Different Numbers of Users and Receiver Antennas . . . . .       | 790 |
| 17.3.2.3.2 | BER Performance of Turbo-Coded PIC Detection-Assisted SDMA-OFDM for Different Numbers of Users and Receiver Antennas . . . . .   | 791 |
| 17.3.2.4   | Complexity Analysis . . . . .                                                                                                    | 793 |
| 17.3.2.5   | Summary and Conclusions on PIC Detection . . . . .                                                                               | 795 |
| 17.3.3     | ML Detection . . . . .                                                                                                           | 796 |
| 17.3.3.1   | Standard ML Detection . . . . .                                                                                                  | 797 |
| 17.3.3.1.1 | Representation of the Vector of Received Signals as a Sample of a Multi-Variate Complex Gaussian Distribution Function . . . . . | 797 |
| 17.3.3.1.2 | Determination of the Vector of Transmitted Symbols by Maximising the <i>A Posteriori</i> Probability . . . . .                   | 798 |
| 17.3.3.2   | Transform-Based ML Detection . . . . .                                                                                           | 799 |
| 17.3.3.3   | ML-Assisted Soft-Bit Generation for Turbo-Decoding . . . . .                                                                     | 801 |
| 17.3.3.3.1 | Standard ML-Assisted Soft-Bit Generation . . . . .                                                                               | 801 |
| 17.3.3.3.2 | Simplification by Maximum Approximation . . . . .                                                                                | 802 |
| 17.3.3.4   | Performance Analysis . . . . .                                                                                                   | 803 |
| 17.3.3.4.1 | BER Performance of ML Detection-Assisted SDMA-OFDM for Different Numbers of Users and Reception Antennas . . . . .               | 803 |
| 17.3.3.4.2 | BER Performance of Turbo-Coded ML Detection-Assisted SDMA-OFDM for Different Numbers of Users and Reception Antennas . . . . .   | 804 |
| 17.3.3.5   | Complexity Analysis . . . . .                                                                                                    | 805 |
| 17.3.3.5.1 | Complexity of Standard ML Detection . . . . .                                                                                    | 806 |

|            |                                                                                                       |     |
|------------|-------------------------------------------------------------------------------------------------------|-----|
| 17.3.3.5.2 | Complexity of Transform-Based ML Detection                                                            | 806 |
| 17.3.3.5.3 | Complexity of ML-Assisted Maximum Approximation Based Soft-Bit Generation                             | 807 |
| 17.3.3.6   | Summary and Conclusions on ML Detection                                                               | 808 |
| 17.3.4     | Final Comparison of the Different Detection Techniques                                                | 809 |
| 17.3.4.1   | BER Performance Comparison of the Different Detection Techniques in Uncoded and Turbo-Coded Scenarios | 809 |
| 17.3.4.2   | Complexity Comparison of the Different Detection Techniques                                           | 811 |
| 17.4       | Performance Enhancement                                                                               | 813 |
| 17.4.1     | Adaptive Modulation-Assisted SDMA-OFDM                                                                | 813 |
| 17.4.1.1   | Outline of the Adaptive Single-User Receiver                                                          | 814 |
| 17.4.1.2   | Outline of the Adaptive Multi-User SDMA-OFDM Receiver                                                 | 814 |
| 17.4.1.3   | Performance Assessment                                                                                | 816 |
| 17.4.1.4   | Summary and Conclusions                                                                               | 818 |
| 17.4.2     | Walsh-Hadamard Transform Spreading Assisted SDMA-OFDM                                                 | 819 |
| 17.4.2.1   | Outline of WHTS-Assisted Single User OFDM Receiver                                                    | 819 |
| 17.4.2.1.1 | Properties of the Walsh-Hadamard Transform                                                            | 820 |
| 17.4.2.1.2 | Receiver Design                                                                                       | 821 |
| 17.4.2.2   | Outline of the WHTS Assisted Multi-User SDMA-OFDM Receiver                                            | 824 |
| 17.4.2.3   | Performance Assessment                                                                                | 826 |
| 17.4.2.3.1 | Single-User WHTS-OFDM                                                                                 | 826 |
| 17.4.2.3.2 | Multi-User SDMA-WHTS-OFDM                                                                             | 828 |
| 17.4.2.4   | Summary and Conclusions                                                                               | 829 |
| 17.5       | Chapter Summary and Conclusion                                                                        | 830 |
| 17.5.1     | Review of the Motivation for Multiple Reception Antenna SDMA Receivers                                | 831 |
| 17.5.2     | Summary and Conclusions Related to Linear Detectors                                                   | 832 |
| 17.5.3     | Summary and Conclusions Related to Non-Linear Detectors                                               | 833 |
| 17.5.3.1   | SIC Detection                                                                                         | 833 |
| 17.5.3.2   | PIC Detection                                                                                         | 835 |
| 17.5.3.3   | ML Detection                                                                                          | 836 |
| 17.5.3.4   | Overall Comparison of the Different Detection Techniques                                              | 837 |
| 17.5.3.5   | Summary and Conclusions Related to Performance Enhancement Techniques                                 | 838 |
| 17.5.3.5.1 | Adaptive Modulation Assisted SDMA-OFDM                                                                | 838 |
| 17.5.3.5.2 | Walsh-Hadamard Transform Spreading Assisted SDMA-OFDM                                                 | 839 |
| 17.6       | List of Symbols Used in Chapter 17                                                                    | 840 |
| 18         | OFDM-Based Wireless Video System Design                                                               | 849 |
| 18.1       | Adaptive Turbo-coded OFDM-Based Videotelephony                                                        | 849 |
| 18.1.1     | Motivation and Background                                                                             | 849 |
| 18.1.2     | AOFD Modem Mode Adaptation and Signalling                                                             | 851 |
| 18.1.3     | AOFD Sub-band BER Estimation                                                                          | 851 |

|           |                                                                                                                 |            |
|-----------|-----------------------------------------------------------------------------------------------------------------|------------|
| 18.1.4    | Video Compression and Transmission Aspects . . . . .                                                            | 852        |
| 18.1.5    | Comparison of Sub-band-Adaptive OFDM and Fixed Mode<br>OFDM Transceivers . . . . .                              | 852        |
| 18.1.6    | Sub-band-Adaptive OFDM Transceivers Having Different<br>Target Bit Rates . . . . .                              | 858        |
| 18.1.7    | Time-Variant Target Bit Rate OFDM Transceivers . . . . .                                                        | 862        |
| 18.2      | Multi-user OFDM/H.263 HIPERLAN-like Video Telephony . . . . .                                                   | 870        |
| 18.2.1    | Overview . . . . .                                                                                              | 870        |
| 18.2.2    | The Video System . . . . .                                                                                      | 871        |
| 18.2.2.1  | OFDM Transceiver . . . . .                                                                                      | 871        |
| 18.2.2.2  | Video Transmission Regime . . . . .                                                                             | 873        |
| 18.2.3    | The OFDM Signal Model . . . . .                                                                                 | 874        |
| 18.2.4    | Co-Channel Interference Cancellation Techniques . . . . .                                                       | 876        |
| 18.2.5    | Video System Performance Results . . . . .                                                                      | 878        |
| 18.3      | Chapter Summary and Conclusion . . . . .                                                                        | 880        |
| <b>19</b> | <b>Conclusion and Further Research Problems</b> . . . . .                                                       | <b>887</b> |
| 19.1      | Summary of Part I . . . . .                                                                                     | 887        |
| 19.1.1    | Summary of Part I . . . . .                                                                                     | 887        |
| 19.1.2    | Conclusions of Part I . . . . .                                                                                 | 888        |
| 19.2      | Summary and Conclusions of Part II . . . . .                                                                    | 889        |
| 19.2.1    | Summary of Part II . . . . .                                                                                    | 889        |
| 19.2.2    | Conclusions of Part II . . . . .                                                                                | 891        |
| 19.3      | Summary and Conclusions of Part III . . . . .                                                                   | 898        |
| 19.3.1    | Pilot-Assisted Channel Estimation for Single-User OFDM . . . . .                                                | 898        |
| 19.3.2    | Decision-Directed Channel Estimation for Single-User OFDM . . . . .                                             | 899        |
| 19.3.2.1  | Complexity Reduction by CIR-Related Domain Filtering . . . . .                                                  | 900        |
| 19.3.2.2  | Compensation of the Channel's Time-Variance by CIR-<br>Related Tap Prediction Filtering . . . . .               | 901        |
| 19.3.2.3  | Subject for Future Research: Successive Adaptivity of<br>KLT and CIR-Related Tap Prediction Filtering . . . . . | 902        |
| 19.3.3    | Channel Estimation for Multi-User SDMA-OFDM . . . . .                                                           | 903        |
| 19.3.3.1  | LS-Assisted DDCE . . . . .                                                                                      | 904        |
| 19.3.3.2  | PIC-Assisted DDCE . . . . .                                                                                     | 904        |
| 19.3.4    | Uplink Detection Techniques for SDMA-OFDM . . . . .                                                             | 906        |
| 19.3.4.1  | SIC Detection . . . . .                                                                                         | 906        |
| 19.3.4.2  | PIC Detection . . . . .                                                                                         | 907        |
| 19.3.4.3  | Improvement of MMSE and PIC Detection by Adaptive<br>Modulation or WHT Spreading . . . . .                      | 907        |
| 19.3.5    | OFDM-Based Wireless Video System Design . . . . .                                                               | 907        |
| 19.4      | Closing Remarks . . . . .                                                                                       | 908        |
|           | <b>Glossary</b> . . . . .                                                                                       | <b>911</b> |
|           | <b>Bibliography</b> . . . . .                                                                                   | <b>915</b> |
|           | <b>Subject Index</b> . . . . .                                                                                  | <b>949</b> |

## **CONTENTS**

---

**xxvii**

## **Author Index**

**965**