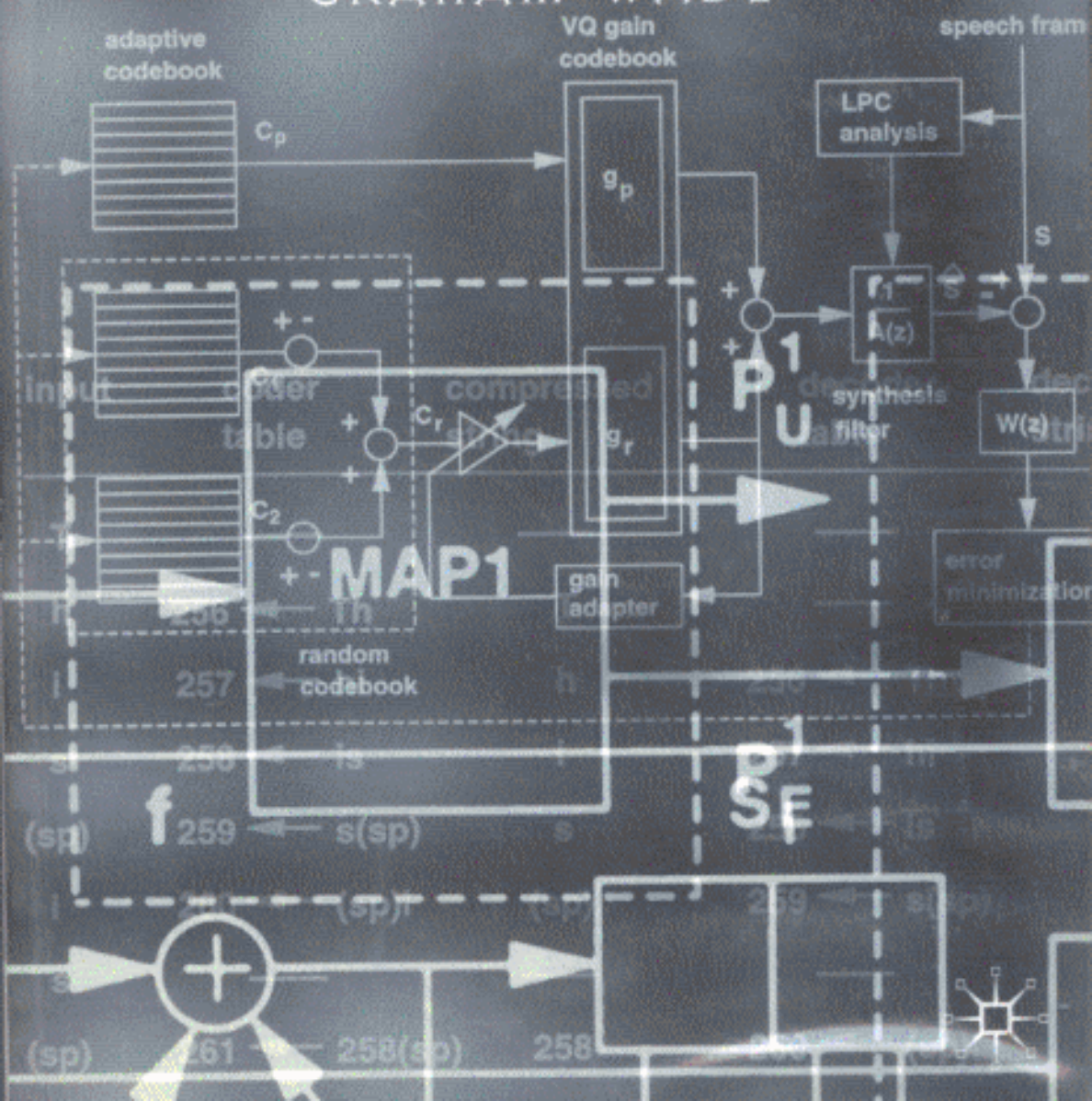


CODING TECHNIQUES

AN INTRODUCTION TO COMPRESSION
AND ERROR CONTROL

GRAHAM WADE



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