

INTERNATIONAL STUDENT EDITION

PROBABILITY  
AND  
STATISTICS

FOR ENGINEERING  
AND THE SCIENCES

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SIXTH EDITION

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