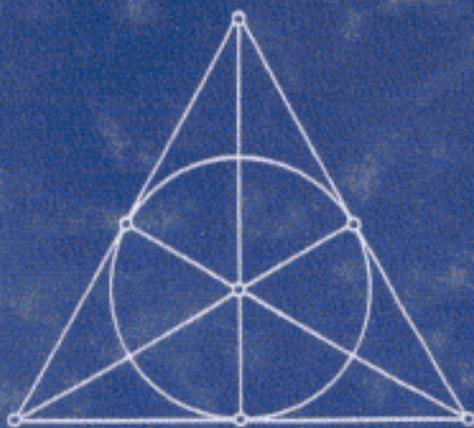


Wiley-Interscience Series in Discrete Mathematics and Optimization

COMBINATORICS

SECOND EDITION



RUSSELL MERRIS

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