Series on Advances in Mathematics for Applied Sciences – Vol. 64

GENERALIZED KINETIC MODELS IN APPLIED SCIENCES

Lecture Notes on Mathematical Problem

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World Scientific

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