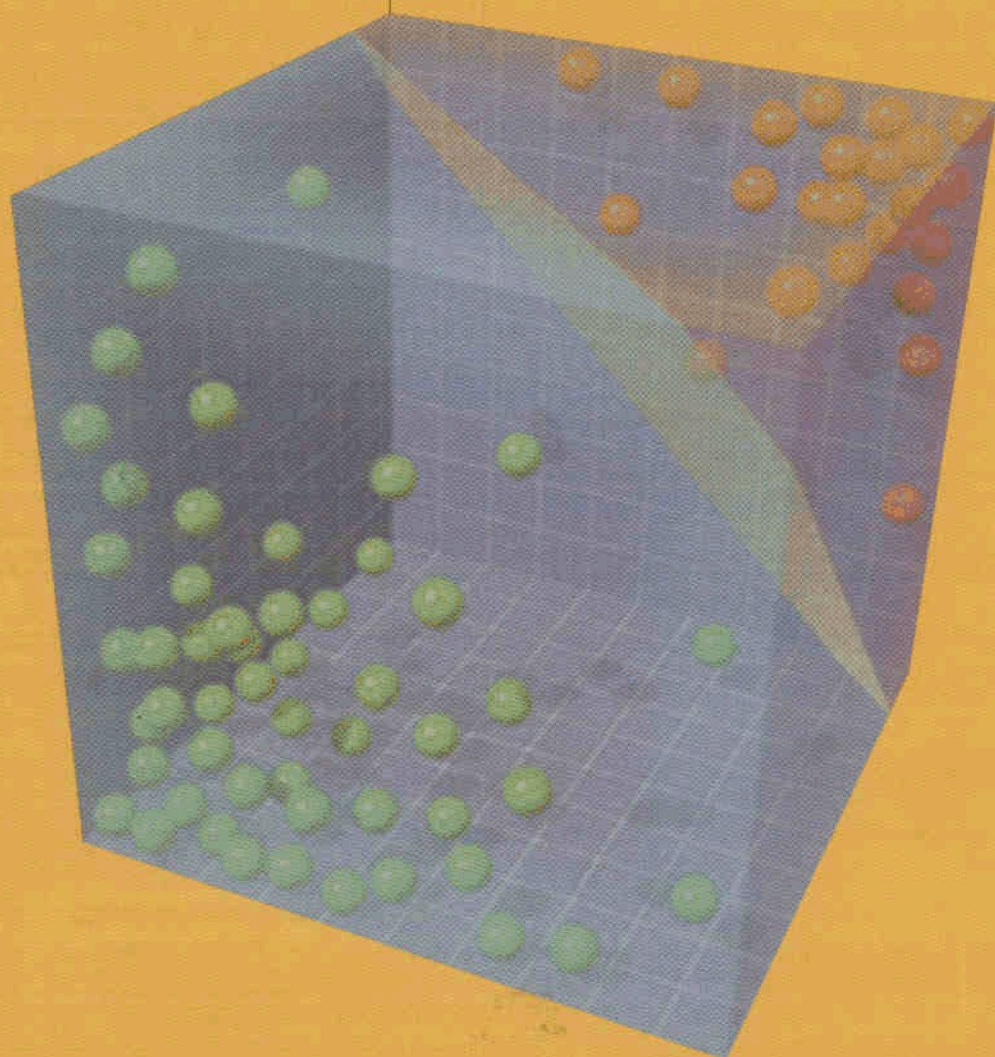


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An Introduction to

Support Vector Machines

and other kernel-based
learning methods



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