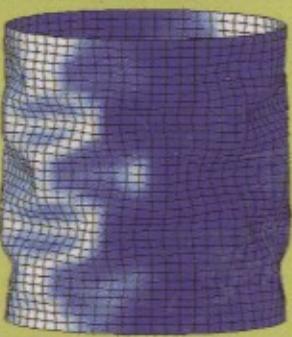


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# Encyclopedia of Computational Mechanics

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Volume 2

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Fundamentals

Solids and Structures

Fluids

 WILEY

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