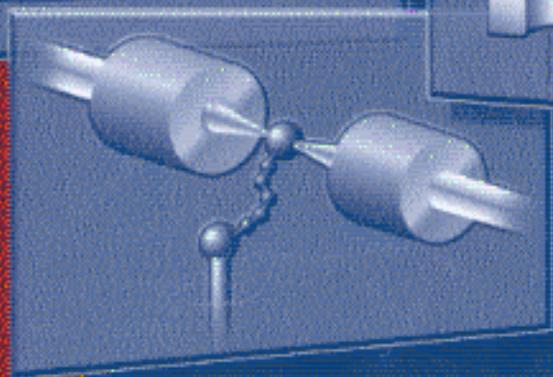
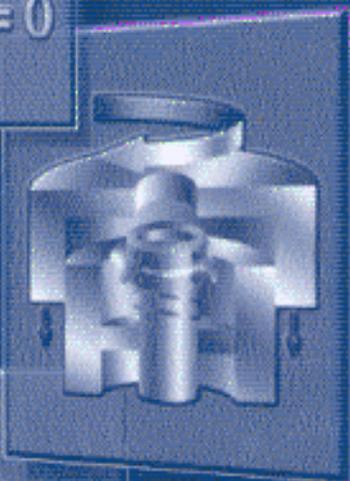


AN INTRODUCTION TO

Biomechanics

Statics and Dynamics
Analysis and Design

$$\frac{\partial \sigma_{xx}}{\partial x} + \frac{\partial \sigma_{yx}}{\partial y} = 0$$



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