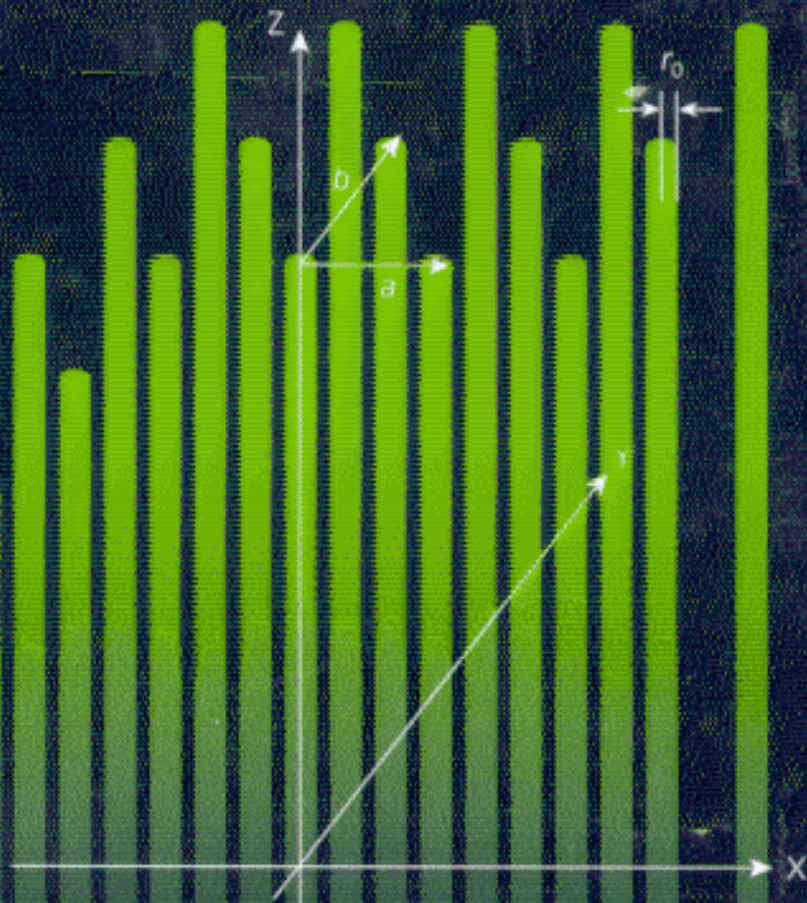


Sergei Tretyakov



ANALYTICAL MODELING IN

**Applied
Electromagnetics**

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