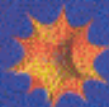
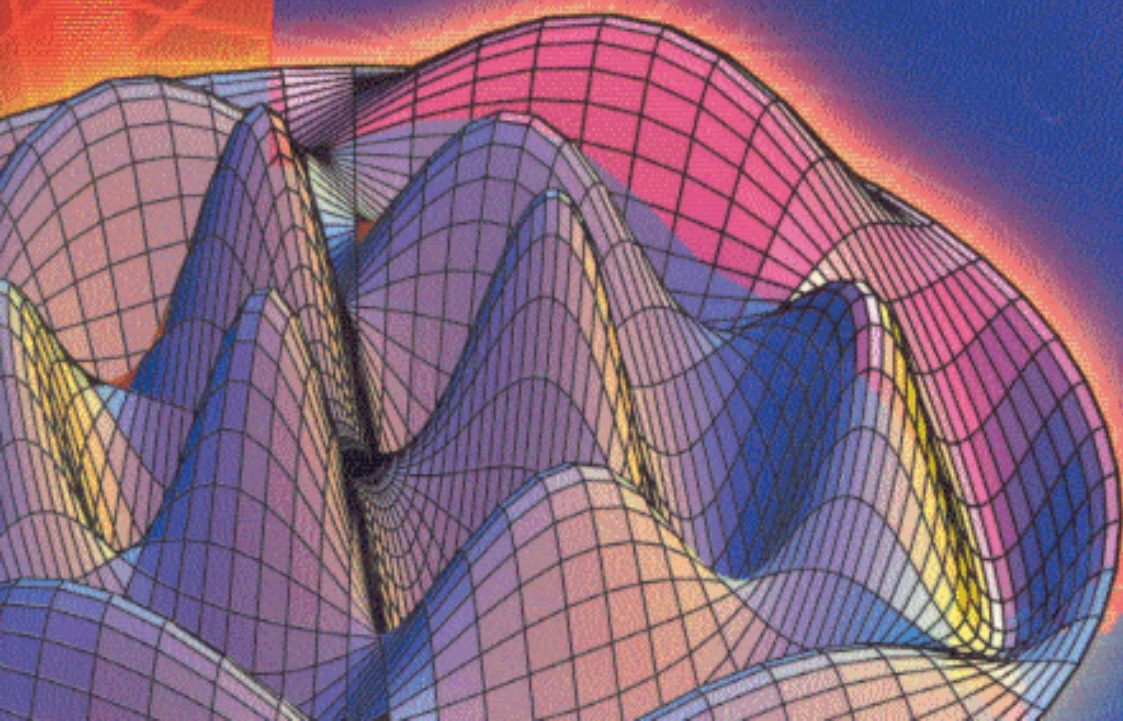




MATHEMATICA by EXAMPLE

Martha L. Abell
James P. Braselton

3rd Edition



MATHEMATICA 5

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