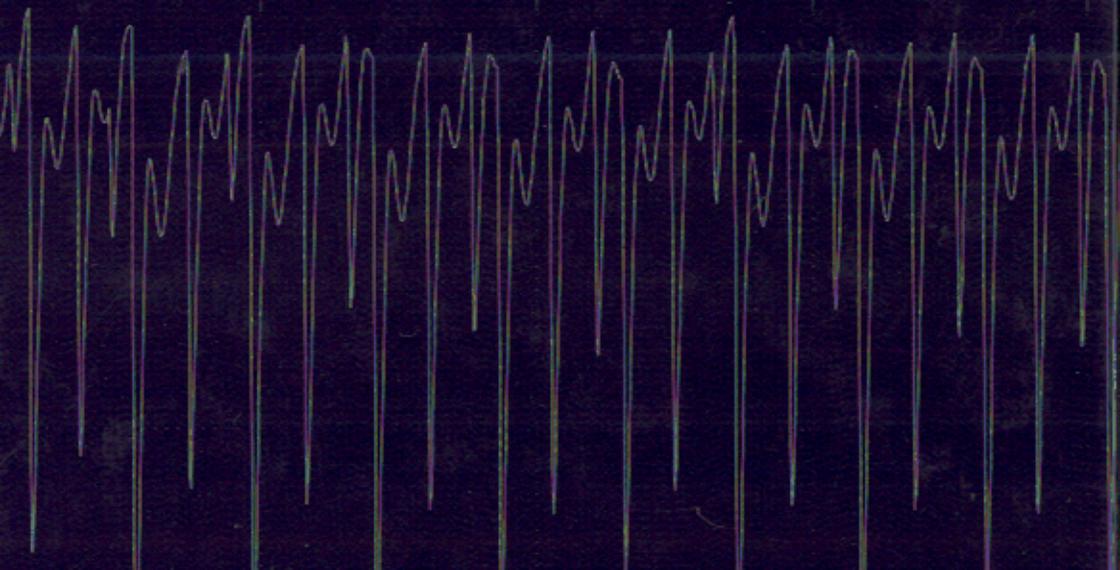




 WILEY

**AN INTRODUCTION TO  
NUMERICAL ANALYSIS FOR  
ELECTRICAL AND COMPUTER ENGINEERS**

**CHRISTOPHER J. ZAROWSKI**



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