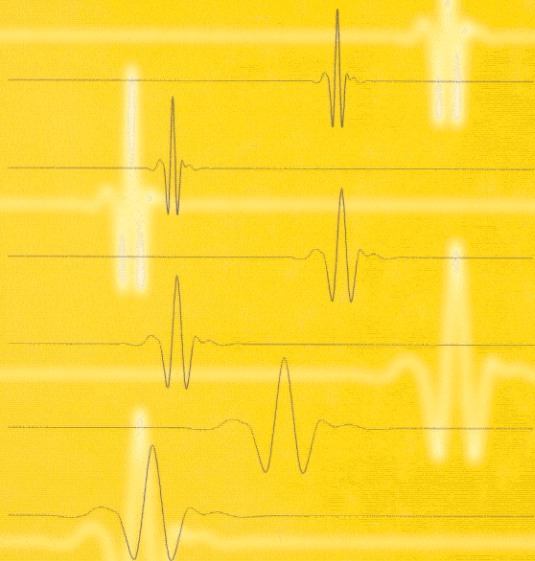


*Chemical Analysis: A Series of Monographs on
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Chemometrics

From Basics to Wavelet Transform

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