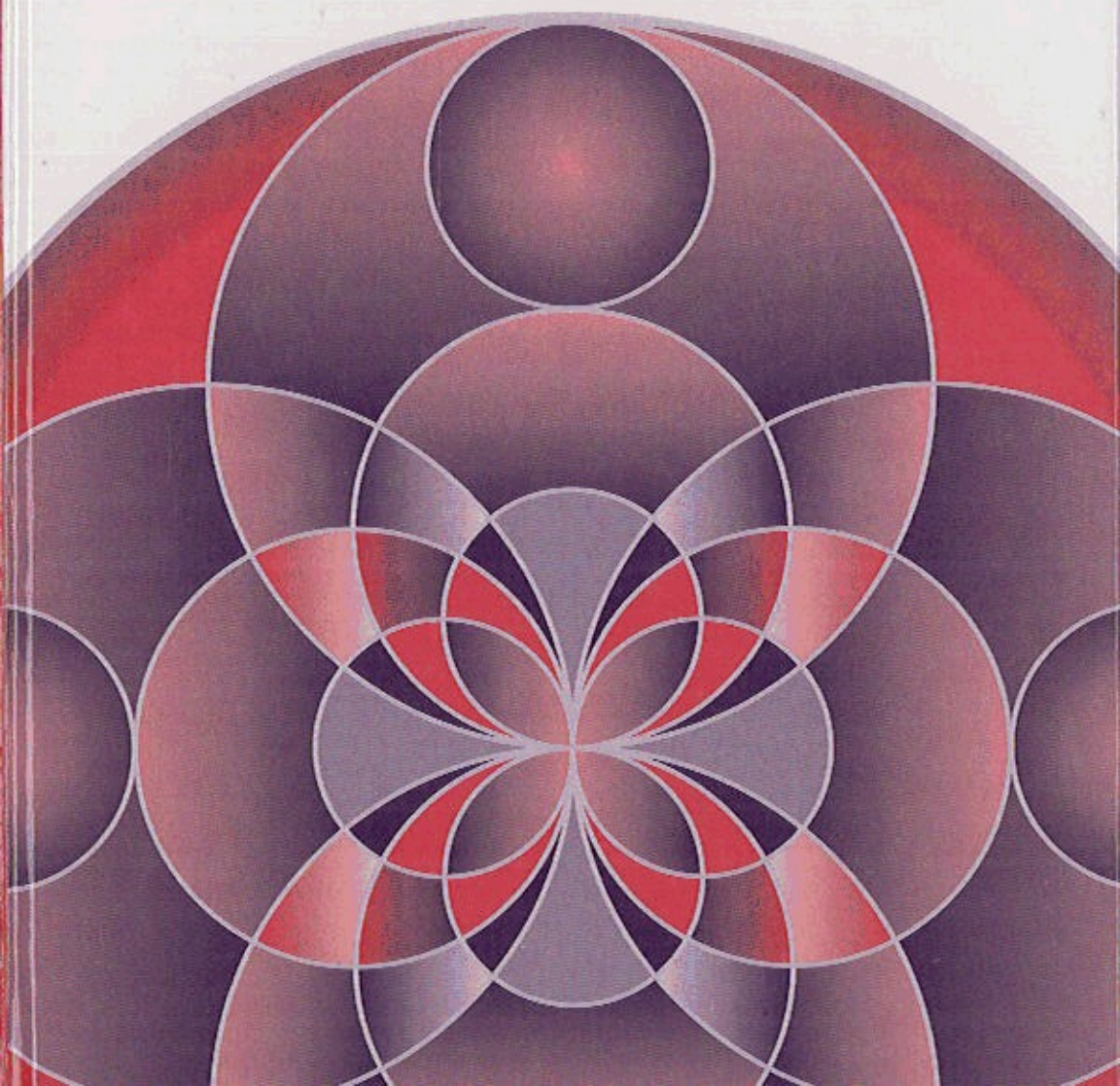


JOEL S. COHEN

**COMPUTER ALGEBRA AND
SYMBOLIC COMPUTATION**

Mathematical Methods



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