

**CONTROL  
ENGINEERING**

Warren E. Dixon

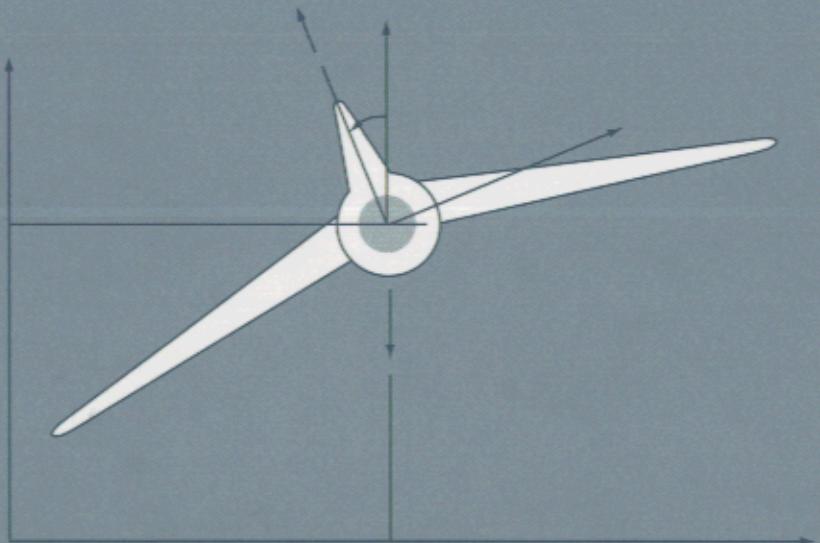
Aman Behal

Darren M. Dawson

Siddharth P. Nagarkatti

# Nonlinear Control of Engineering Systems

A Lyapunov-Based Approach



Birkhäuser

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