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Large Eddy Simulation for Incompressible Flows

Scientific
Computation

An Introduction

Second Edition



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