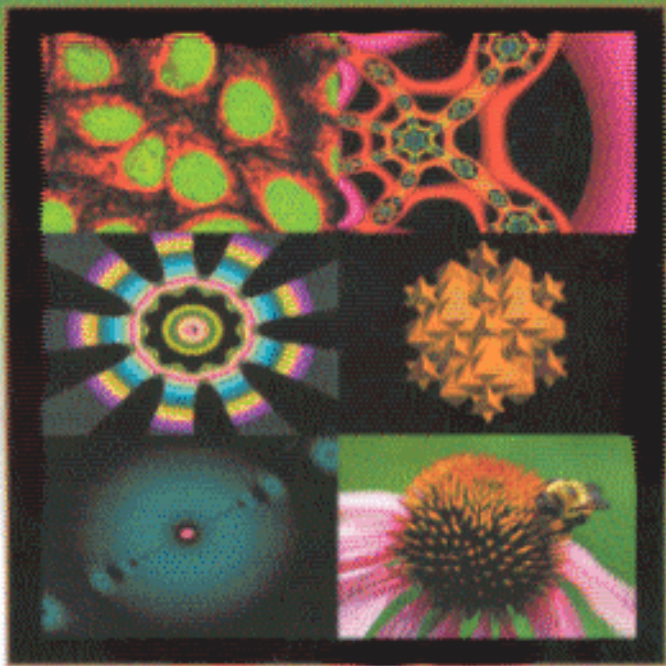


SECOND EDITION

# Nano- and Micro-Electromechanical Systems

Fundamentals of  
Nano- and Microengineering



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