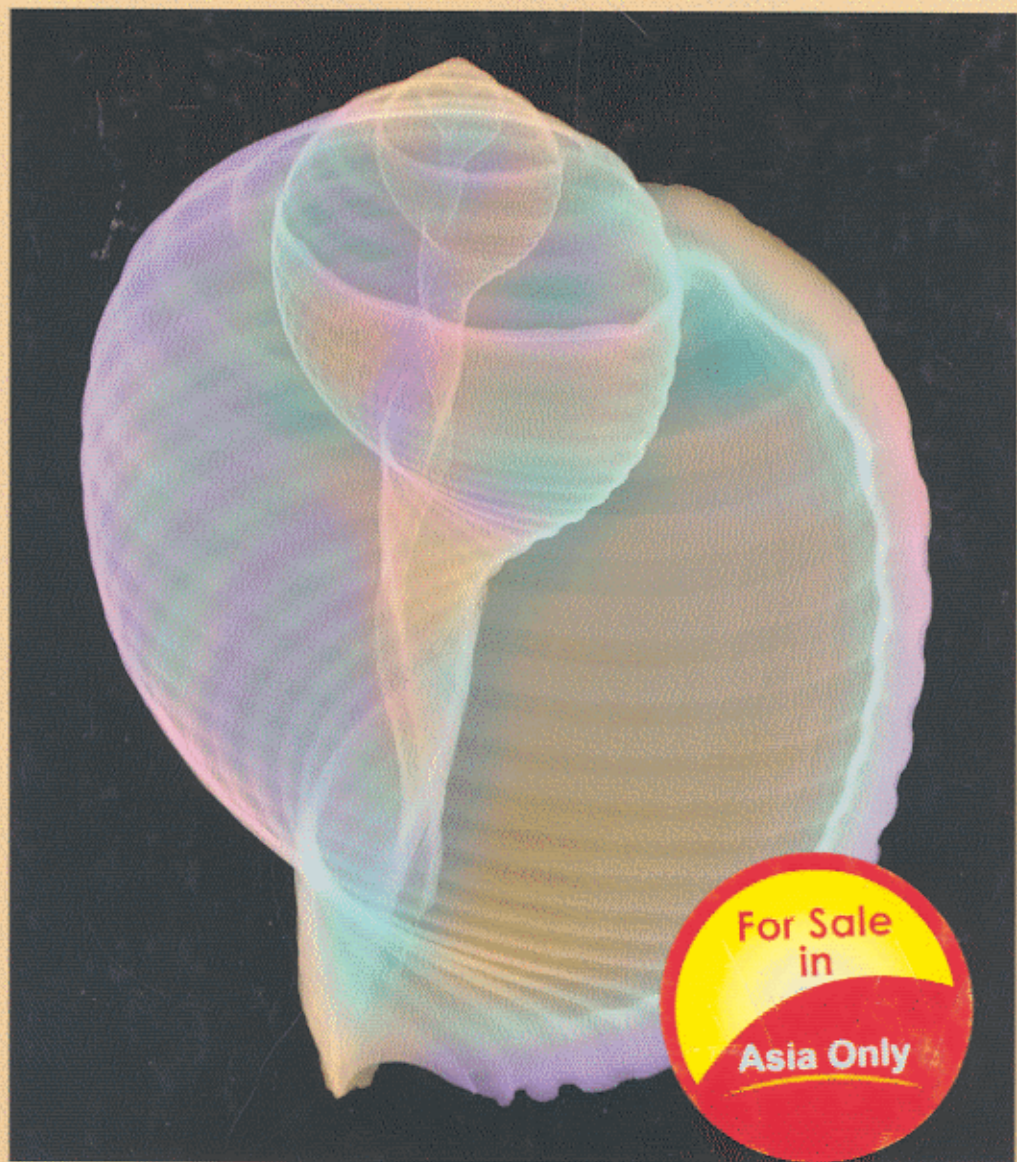


# Introduction to Mathematical Statistics

Sixth Edition



For Sale  
in

Asia Only

Hogg · McKean · Craig

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