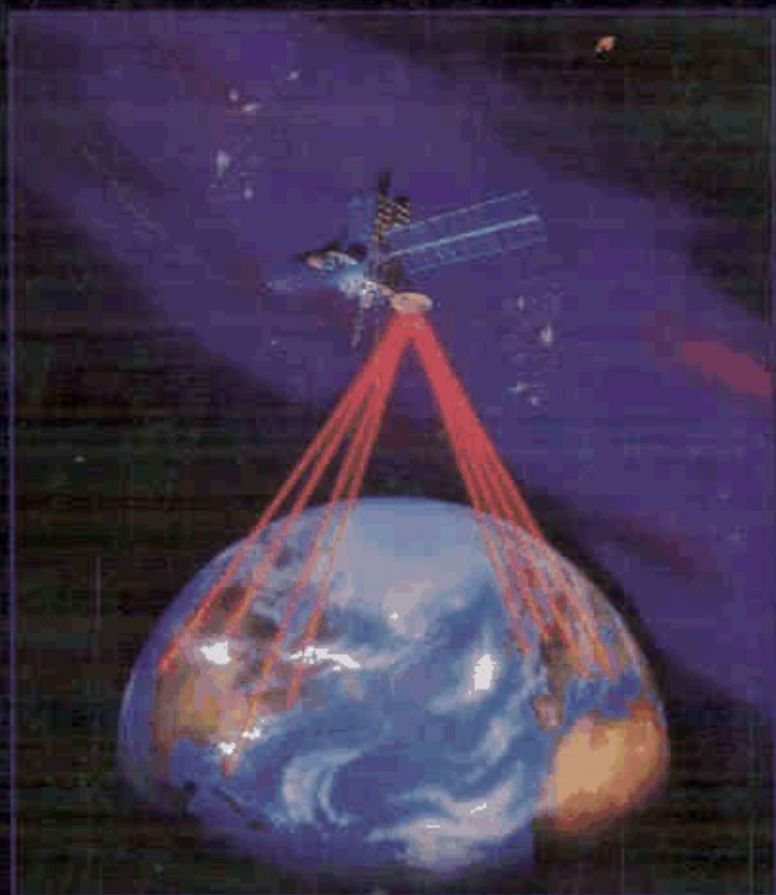


INTERNATIONAL EDITION

Fundamentals of Complex Analysis

with Applications to Engineering and Science

Third Edition



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