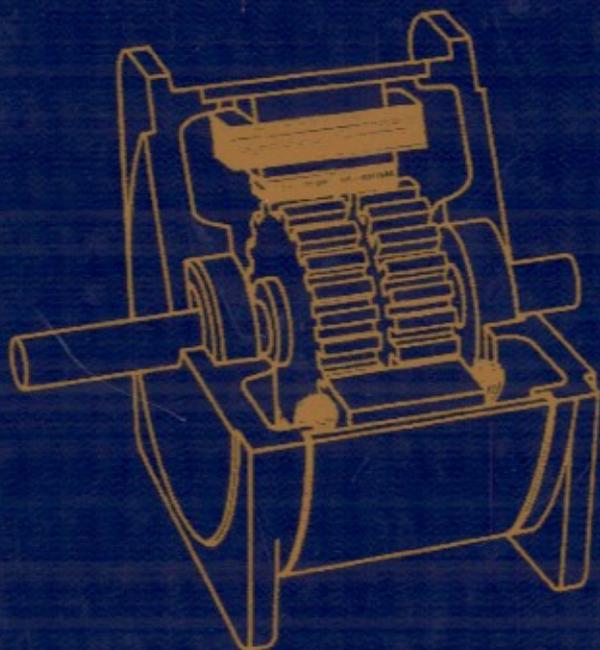


IEEE Series on Power Engineering

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Modeling and High-Performance Control of Electric Machines



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JOHN CHIASSON

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