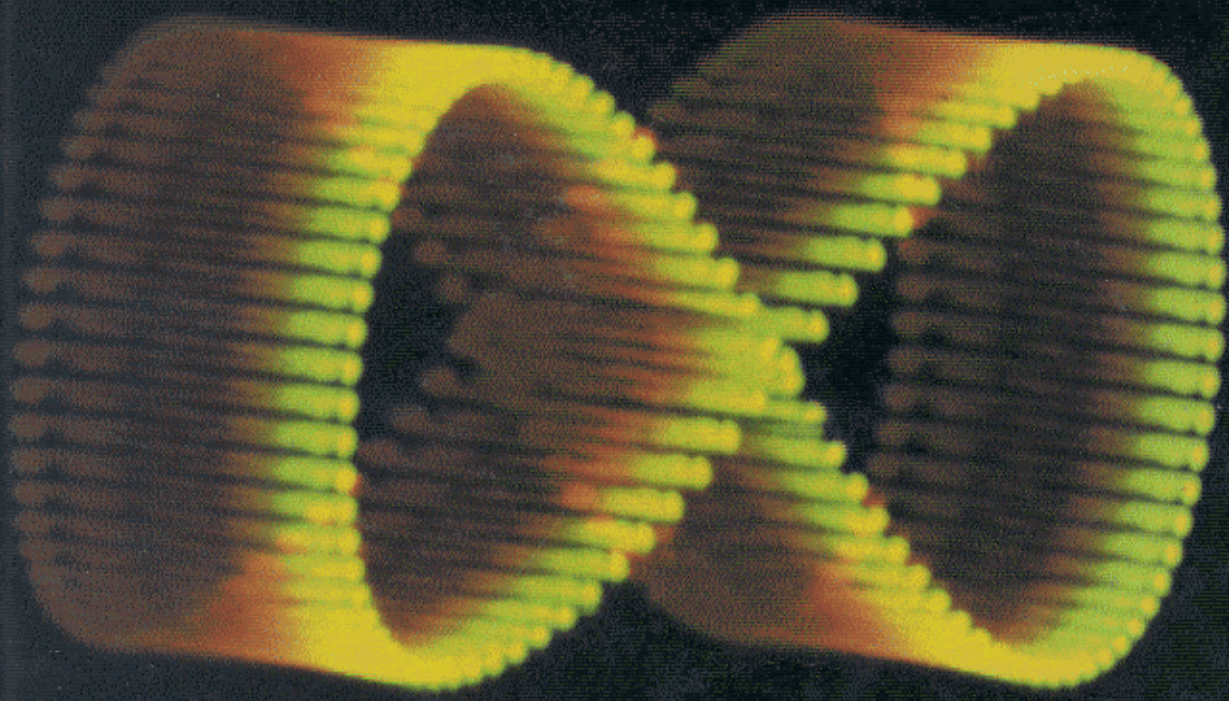
C. L. Tang

Fundamentals of Quantum Mechanics

For Solid State Electronics and Optics



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